This is a full length practice midterm exam. If you want to take it at exam pace, give yourself 75 minutes to take the entire test. Just like the real exam, each question has a point value. There are 75 points from 6 question, so pace yourself accordingly.

Questions:

1. Combinatorial Logic: 15 pts
2. Sequential Logic: 10 pts
3. FSMs: 10 pts
4. Asm Programming: 20 pts
5. Datapaths: 10 pts
6. Memory Hierarchy: 10 pts
Question 1 Combinatorial Logic [15 pts]
Given the following truth-table:

<table>
<thead>
<tr>
<th>a</th>
<th>b</th>
<th>c</th>
<th>x</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
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</table>

1. Write the sum-of-product formula

2. Simplify the formula

3. Write VHDL that implements the formula

```vhdl
entity q1 is
    port (a : in std_logic; b : in std_logic; c : in std_logic; x : out std_logic);
end q1;
architecture basic of q1 is
begin
end basic;
```
**Question 2 Sequential Logic [10 pts]**

Consider the following VHDL fragment, in which \( x \), and \( y \) are inputs, \( z \) is an output, and there are two DFFs (\( a \) and \( b \)) whose \( d \) inputs are \( a_d \) and \( b_d \) respectively, and whose \( q \) outputs are \( a_q \) and \( b_q \) respectively:

\[
\begin{align*}
    b_d &= a_q \text{ xor } x; \\
    a_d &= (b_q \text{ and } a_q) \text{ xor } y; \\
    z &= a_q \text{ xor } b_q;
\end{align*}
\]

Complete the waveform below (assume that the DFFs are triggered by the rising edge of \( \text{clk} \)): Note that \( a_q \) is initially 1, and \( b_q \) is initially 0:

<table>
<thead>
<tr>
<th>clk</th>
<th>x</th>
<th>y</th>
<th>a_d</th>
<th>a_q</th>
<th>b_d</th>
<th>b_q</th>
<th>z</th>
</tr>
</thead>
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</table>
Question 3 FSMs [10 pts]

Draw a state machine diagram for a finite state machine which accepts a single bit input (either 0 or 1—you can just label each edge with 0 or 1). This state machine also has a single bit of output, which is initially 0.

- Whenever the FSM receives an input bit of 1 followed by anything other than two 0s (so 11, or 101) the output goes to 1.

- The output remains at 1 until 3 consecutive 0s are received by the FSM.

- Once three consecutive 0s are received by the FSM, the output returns to 0.

- The output now remains 0 until it again sees a 1 which is not followed (immediately) by two 0s.

Note that when the FSM sees a 1 not followed by two 0s, the output goes to 1 as soon as the situation is detected (e.g., on the second 1 of 11 or 101). Label each state with the bit it outputs. Be sure to indicate your start state (with an arrow to it from nowhere).
Question 4 Asm Programming [20 pts]

Translate the following C function to MIPS assembly. Answer on the next 2 pages where you have each C-code line written out for you with space to write the MIPS assembly for that line directly under it.

```c
int countMatching(int * ptr, int n) {
    int count = 0;
    while (n > 0) {
        int x = testFn(*ptr);
        if (x != 0) {
            count++;
        }
        ptr++;
        n--;
    }
    return count;
}
```

Answer on next 2 pages
# int countMatching(int * ptr, int n) {

#     int count = 0;

#     while (n > 0) {

#         int x = testFn(*ptr);

#         if (x != 0) {

#             count++;

#         }

#     }

# }
ptr++;

n--;

return count;
Question 5 Datapaths [10 pts]

1. If a single cycle datapath has a clock period of 100ns, and is split into a multi-cycle data path with 5 stages, the clock will be slower than 20ns. Give two reasons why:

   •

   •

2. In the 1990s, processor design was about “performance at all cost,” however now, performance must be balanced against other design considerations. Name two such design considerations, and for each one explain (briefly) why it is important.

   •

   •
Question 6 Memory Hierarchy [10 pts]

A processor uses 12-bit addresses, and has a 64-byte direct-mapped cache. The cache is organized in 8 sets, with 8-bytes per block. The contents of the cache are shown below:

<table>
<thead>
<tr>
<th>Set</th>
<th>Tag</th>
<th>Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0F</td>
<td>1F 12 34 56 78 99 43 59 B3</td>
</tr>
<tr>
<td>1</td>
<td>15</td>
<td>11 12 22 33 44 B4 C6 A9 D2</td>
</tr>
<tr>
<td>2</td>
<td>31</td>
<td>2F 3E 4D 5C A0 C9 DA 9C</td>
</tr>
<tr>
<td>3</td>
<td>15</td>
<td>37 83 A9 C0 3F F3 2C AE</td>
</tr>
<tr>
<td>4</td>
<td>3E</td>
<td>FF EE DD CC F9 F8 7C 8D</td>
</tr>
<tr>
<td>5</td>
<td>1C</td>
<td>1F 1E 1D 1C 1B 1A 10 19</td>
</tr>
<tr>
<td>6</td>
<td>0A</td>
<td>F6 D7 C8 E9 00 01 02 03</td>
</tr>
<tr>
<td>7</td>
<td>0A</td>
<td>77 66 55 AA 05 06 07 08</td>
</tr>
</tbody>
</table>

Note that the least-significant byte in each block is on the right, and the most-significant is on the left (so in the first block, byte 0 is B3 and byte 7 is 12).

For each of the following addresses (a) split the address into tag/index/offset and write them in hex (b) determine if the access is a hit or miss (c) if the access is a hit, write the data that a 1-byte load to that address returns (if it is a miss, leave that field blank):

1. 0x55E
   - Tag:
   - Index:
   - Offset:
   - Hit or miss?
   - Value loaded:

2. 0x297
   - Tag:
   - Index:
   - Offset:
   - Hit or miss?
   - Value loaded: