Collateral and Secured Debt

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Theory to Distinguish between Secured Debt and Collateral

Secured debt

- Explicit collateralization: lien on specific assets, recovered in default
- Secured lenders' strong claim on assets enables higher leverage
- Entails costs: direct or indirect (operational flexibility)

Unsecured debt

Backed by unencumbered assets, implicitly collateralized

Key insights

- Collateral restricts both secured and unsecured debt
- Constrained firms use more secured debt within and across firms

Consistent with stylized facts and evidence from causal forest

- Bulk of debt secured for most firms
- Positive relation between secured debt and financial constraints
- Positive relation between leverage and tangible assets

Why Do We Care?

Collateral central to macro finance and corporate finance

- Kiyotaki/Moore (1997)
- Rampini/Viswanathan (2013)

Recent puzzles on secured debt

- Secured debt acyclical/countercyclical Azariadis/Kass/Wen (2016)
 - Relatedly: leasing countercyclical Gal/Pinter (2017)
- Limited use of secured debt by large firms Lian/Ma (2021)
- Secular decline in secured debt Benmelech/Kumar/Rajan (2021)
- No distinction between secured debt and collateral!

Terminology

- Collateral (law): Assets pledged to secure loan
- **Collateral (economics):** Collateralizable assets, esp. tangible assets

Punchline

Collateral is essential to understanding capital structure

Law Perspective on Secured Debt

Based on Mann (1997)

Benefits of secured debt: enforcement of payment

- "increases the lender's ability to collect the debt forcibly through liquidation of the collateral"
- "enhances the lender's remedy (so that the lender can coerce payment more quickly than it could if its debt were not secured)"

Costs of secured debt

- Direct costs, such as information and transactions costs
- Indirect costs, such as operating flexibility

"you just don't have the same flexibility of dealing with your properties as if you owned them unencumbered"

Very similar to basic trade-off in our model

Law Perspective on Secured Debt

Trade off depends on firms' financial condition

- "as a borrower's financial strength increases, secured credit becomes a less attractive alternative: its benefits decrease and its costs at best, remain constant" – Mann (1997)
- "borrowers exhibit an increasing tendency toward unsecured debt as their financial strength increases" - Mann (1997)
- "unsecured creditors frequently choose to waive negative pledge covenants in exchange for a quid pro quo, such as becoming equally and ratably secured" – Schwarcz (1997)

Contracting in the shadow of the law

 Borrowers and lenders are "reacting to the 'shadow' of the law – the parties' anticipation of what would happen if formal legal proceedings were to occur" – Mann (1997)

Outline

- (1) Stylized facts
- (2) Model
 - Key distinction between secured and unsecured debt
 - Simple, deterministic model
 - Stochastic model with quantitative evaluation
- (3) Secured debt and leasing (skipped today)
- (4) Evidence from causal forest

Stylized Facts on Secured Debt

Data

- Compustat; 1981-2018; annual; excluding SIC 6000-6999
- Secured debt: Debt/Mortgages & Other Secured (DM)
- **Debt:** Long-Term Debt (DLTT) + Debt in Current Liabilities (DLC)
- Assets: Assets (AT)
- Two key stylized facts
 - **Fact 1:** Secured debt increases with financial constraints
 - Fact 2: Leverage increases with tangible assets

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■ Financial structure across rating deciles Model Long-term debt



Panel C: Unsecured debt/Assets

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tq 0.4 0.3 0.2





Cross section: constrained firms have more secured debt Assets & Div

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Credit rating deciles

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Within-firm variation: heterogeneous effects of downgrades



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Collateral and Secured Debt

Shift to secured debt, esp. low-rated firms



Financial structure and assets across size deciles



8 9

5

Assets deciles

0.3 0.2 0.1

1 2 3 4

Panel B: Secured debt/Total debt





Small (financially constrained) firms high fraction secured Assets & Div

Stylized Fact 2 – Financial Structure and Tangible Assets

Financial structure and assets across tangibility deciles



Panel C: Unsecured debt/Assets

Panel B: Secured debt/Total debt



Panel D: Debt/Assets



Secured debt and total leverage increase substantially with tangibility

Stylized Facts - Secured Long-Term Debt Ratio

Ratio of secured debt to long-term debt



Panel C: Δ Secured LT debt ratio



Panel B: Secured LT debt ratio by assets



Panel D: Secured LT debt ratio by tangibility



Patterns in secured LT debt still more pronounced

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Collateral and Secured Debt

Model with Secured and Unsecured Debt

Environment

- Discrete time, infinite horizon: $t = 0, 1, 2, \ldots$
- Risk-neutral firm discounts at rate $\beta \in (0, 1)$; limited liability
- Net worth w_0 at time 0
- Two types of capital: tangible and intangible (fixed proportions)
- Leontief aggregator $k \equiv \min\{k_p/\varphi, k_i/(1-\varphi)\}; \ \varphi \in (0,1]$ tangible
- \blacksquare Capital k yields cash flow A(z')f(k) with productivity A(z')
- $\blacksquare \ z'$ follows Markov chain with transition function $\Pi(z,z')$ on $z'\in Z$
- \blacksquare Capital k depreciates at rate $\delta \in (0,1)$
- Production function
 - Decreasing returns and Inada condition
 - Assumption 1. Production function f strictly increasing, strictly concave, f(0) = 0, $\lim_{k\to 0} f'(k) = +\infty$, and $\lim_{k\to +\infty} f'(k) = 0$

Secured vs. Unsecured Debt

- Financing
 - \blacksquare Intangible capital $(1-\varphi)k$ internally financed
 - \blacksquare Tangible capital φk can be financed with secured and unsecured debt
 - \blacksquare Encumbered capital k_s explicitly pledged to secured lender
 - \blacksquare Unencumbered capital $k_u = \varphi k k_s$ backs unsecured debt
- Collateralizability θ_s and cost κ of secured debt Mann (1997)
 - Benefit: "increas[es] the lender's ability to collect the debt forcibly through liquidation of the collateral" and "enhanc[es] the lender's remedy (so that the lender can coerce payment more quickly than it could if its debt were not secured)"
 - Cost (direct and indirect): "[y]ou just don't have the same flexibility of dealing with your properties as if you owned them unencumbered"
 - Assumption 2. $1 > \theta_s > \theta_u \ge 0$ and $\kappa > 0$
- Benefits and costs of secured and unsecured debt
 - Assumption 3. $R^{-1}(\theta_s \theta_u)(1 \delta) > \kappa > (R^{-1} \beta)(\theta_s \theta_u)(1 \delta)$
- Alternative: encumbered capital less efficient (indirect cost)

•
$$\varphi k = k_u + \phi k_s$$
 with $\phi < 1$

Deterministic Model with Secured & Unsecured Debt

- Simplified model without uncertainty
 - No uncertainty (A' constant); no intangible capital ($\varphi = 1$)

Firm's problem

$$v(w) = \max_{\{d,k_s,k_u,w',b'_s,b'_u\} \in \mathbb{R}^4_+ \times \mathbb{R}^2} d + \beta v(w')$$
(1)

subject to budget constraints for current and next period

$$w + \sum_{j \in \mathcal{J}} b'_{j} \geq d + \sum_{j \in \mathcal{J}} k_{j} + \kappa k_{s}$$
(2)
$$A' f \Big(\sum_{j \in \mathcal{J}} k_{j} \Big) + \sum_{j \in \mathcal{J}} k_{j} (1 - \delta) \geq w' + \sum_{j \in \mathcal{J}} R b'_{j}$$
(3)

collateral constraints on secured and unsecured borrowing

$$\theta_j k_j (1-\delta) \ge R b'_j, \qquad \forall j \in \mathcal{J},$$
(4)

where $\mathcal{J} \equiv \{s, u\}$.

Deterministic Model - First-order Conditions

Notation

• Multipliers on constraints (2) to (4): μ , $\beta\mu'$, and $\beta\lambda'_j$

• Multipliers on non-negativity constraints for k_j and d: $\underline{\nu}_j$ and $\underline{\nu}_d$

• Let
$$k \equiv \sum_{j \in \mathcal{J}} k_j$$

First-order conditions

$$\mu = 1 + \underline{\nu}_d \tag{5}$$

$$\mu = \beta R \mu' + \beta R \lambda'_j, \qquad \forall j \in \mathcal{J},$$
(6)

$$\mu(1+\kappa) = \beta \mu' [A' f_k(k) + (1-\delta)] + \beta \lambda'_s \theta_s(1-\delta) + \underline{\nu}_s \quad (7)$$

$$\mu = \beta \mu' [A' f_k(k) + (1-\delta)] + \beta \lambda'_u \theta_u(1-\delta) + \underline{\nu}_u \quad (8)$$

$$\beta \mu' = \beta v_w(w') \quad (9)$$

• Envelope condition: $v_w(w) = \mu$ (marginal value of net worth)

Note:
$$\lambda'_u = \lambda'_s \equiv \lambda'$$

Model with Secured and Unsecured Debt

Down payments and investment Euler equation

• Down pmts: $\wp_s = 1 - R^{-1} \theta_s (1 - \delta) + \kappa$; $\wp_u = 1 - R^{-1} \theta_u (1 - \delta)$

Firm's investment Euler equation (IEE)

$$1 = \beta \frac{\mu'}{\mu} \frac{A' f_k(k) + (1 - \theta_j)(1 - \delta)}{\wp_j} + \frac{\underline{\nu}_j / \mu}{\wp_j}, \qquad \forall j \in \mathcal{J}.$$
(10)

Choice between secured and unsecured debt

Rewrite IEEs using Jorgenson's (1963) frictionless user cost $u \equiv r + \delta$

$$u + R\kappa + R \frac{\lambda'}{\mu'} \wp_s \geq A' f_k(k)$$
 (11)

$$u + R \frac{\lambda'}{\mu'} \wp_u \geq A' f_k(k),$$
 (12)

with equality if $k_j > 0$

- Trade-off between cost of encumbering assets and down payments
- Assumption 3 implies $\wp_s < \wp_u$ (otherwise secured debt dominated)
 - Secured debt enables more borrowing/higher leverage

Model with Secured and Unsecured Debt

Using IEEs we get

$$1 = \beta \frac{\mu'}{\mu} \frac{(\theta_s - \theta_u)(1 - \delta)}{\wp_u - \wp_s} + \frac{\underline{\nu}_u / \mu - \underline{\nu}_s / \mu}{\wp_u - \wp_s}$$
(13)

• Let
$$R_s \equiv \frac{(\theta_s - \theta_u)(1-\delta)}{\wp_u - \wp_s} > R$$
 (by Assumption 2)

- Secured debt is more costly
- Severely constrained firms ($w \rightarrow 0$) use secured debt only

• (2) & (4)
$$\Rightarrow w \ge \sum_{j \in \mathcal{J}} \wp_j k_j$$
 and $k_j \to 0$, $\forall j \in \mathcal{J} \Rightarrow k \to 0$

• IEE implies $\beta\mu'/\mu \rightarrow 0$; then (13) implies $\underline{\nu}_u > 0$

Dividend-paying firms (d > 0) use unsecured debt only

- \blacksquare Firm pays dividends in steady state: $\mu=\mu'=1,$ so $\beta\mu'/\mu=\beta$
- By Assumption 3 $R_s > \beta^{-1}$; then (13) implies $\underline{\nu}_s > 0$

■ IEE:
$$1 = \beta \frac{A' f_k(k) + (1 - \theta_u)(1 - \delta)}{\wp_u}$$
 implicitly defines \bar{k}

Firms indifferent between secured and unsecured debt

From (13):
$$\beta \mu' / \mu = R_s^{-1}$$
; IEE defines $\underline{k} < \overline{k}$

Model with Secured and Unsecured Debt: Characterization

Given Assumptions 1 to 3, \exists thresholds $0 < \underline{w}_s < \bar{w}_s < \bar{w} < +\infty$

Financing policy

- $w \leq \underline{w}_s$: issue only secured debt
- $w \in (\underline{w}_s, \overline{w}_s)$: substitute from secured debt to unsecured debt
- $w \geq \bar{w}_s$: use only unsecured debt
- Investment k increases in w; strictly if $w \leq \underline{w}_s$, $w \in [\overline{w}_s, \overline{w}]$
- **Payout policy:** firms with $w > \overline{w}$ pay dividends
- Firm life cycle
 - Over time, firms accumulate net worth, ...
 - ... increase investment,
 - ... substitute from secured debt to unsecured debt,
 - ... and eventually initiate dividends.

Model with Secured and Unsecured Debt with Uncertainty

Stochastic productivity

- Assumption 4. $\forall z_+, z \in Z \ni z_+ > z$, (i) $A(z_+) > A(z)$, (ii) A(z) > 0
- Firm's problem

$$v(w, z) = \max_{\{d, k_s, k_u, w', b'_s, b'_u\} \in \mathbb{R}^4_+ \times \mathbb{R}^{2S}} d + \beta E[v(w', z')|z]$$
(14)

subject to budget constraints for current and next period, $\forall z' \in Z,$

$$w + E\left[\sum_{j \in \mathcal{J}} b'_{j} \middle| z\right] \geq d + \frac{1}{\varphi} \sum_{j \in \mathcal{J}} k_{j} + \kappa k_{s} \quad (15)$$
$$A' f\left(\frac{1}{\varphi} \sum_{j \in \mathcal{J}} k_{j}\right) + \frac{1}{\varphi} \sum_{j \in \mathcal{J}} k_{j} (1 - \delta) \geq w' + \sum_{j \in \mathcal{J}} Rb'_{j} \quad (16)$$

and collateral constraints (4) $orall \{j, z'\} \in \mathcal{J} imes Z$

Model with Secured and Unsecured Debt

Investment Euler equation (IEE)

$$1 = E \left[\beta \frac{\mu'}{\mu} \frac{A' f_k(k) + (1 - \varphi \theta_j)(1 - \delta)}{\wp_j^{\varphi}} \middle| z \right] + \frac{\varphi \underline{\nu}_j / \mu}{\wp_j^{\varphi}}$$
(17)

where $\wp_{j}^{\varphi}\equiv1-\varphi+\varphi\wp_{j}$

- Severely constrained firms ($w \rightarrow 0$) use secured debt only
 - (15) & (4) $\Rightarrow w \geq \frac{1}{\varphi} \sum_{j \in \mathcal{J}} \wp_j^{\varphi} k_j \Rightarrow k_j \to 0, \forall j \in \mathcal{J}; k \to 0$
 - IEE implies $\beta \mu'/\mu \to 0$, $\forall z' \in Z$ since

$$1 \geq E\left[\beta\frac{\mu'}{\mu}\frac{A'f_k(k) + (1-\varphi\theta_j)(1-\delta)}{\wp_j^{\varphi}}\Big|z\right]$$
$$\geq \beta\frac{\mu'}{\mu}\frac{A'f_k(k) + (1-\varphi\theta_j)(1-\delta)}{\wp_j^{\varphi}}$$

- Analogous argument implies $\underline{\nu}_u > 0$
- Financially constrained firms borrow secured
- Dividend-paying firms use unsecured debt only

Quantitative Evaluation

Baseline calibration based on Li/Whited/Wu (2016)

- Structural estimate version of R/V (2013) model using SMM
- Calibrated parameters:
 - $\beta = 0.985$ avg. real 3m T-bill rate 1965-2012: 1.5%
 - $\blacksquare \ R^{-1} = 0.988$ difference due to tax wedge with $\tau = 20\%$
- Estimated parameters:

•
$$f(k) = k^{\alpha}$$
 and $\alpha = 0.6$

- $A(z') = \exp(z')$ with $\sigma_z = 0.5$ and $\rho_z = 0.5$
- Not used: $\delta = 0.04; \ \theta = 0.4$

Our parametrization

- Symmetric two-state Markov chain with $\Pi(z,z) = 0.75$ to match ρ_z
- $\bullet \ \delta = 0.1$
- $\varphi = 0.6$: Falato/Kadyrzhanova/Sim/Steri (forthcoming)
- Calibrated: $\theta_s = 0.8$; $\theta_u = 0.6$; $\kappa = 0.01$

Quantitative Evaluation



Secured debt and leverage decrease with net worth

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Secured Debt and Leasing (skipped today)



Effect of Downgrades – Inference using Causal Forest 🕬

- **Estimate heterogeneous treatment effects using causal forest**
 - Method: Wager/Athey (2018); Athey/Wager (2019)
 - Application to covenant violations: Gulen/Jens/Page (2021)

Primer on causal forest

- Non-parametric machine learning based estimation method
- Intuitively: nearest neighbor method with adaptive neighborhood
- Classification and regression trees (CARTs): tree with leaves
 - Grow tree by recursively splitting sample by covariates
 - Maximize variance of treatment effects across leaves
- Honest (causal) tree splits sample into training and estimation set
- Causal forest aggregates causal trees to allow inference
 - Obtain consistent, asymptotically normal treatment effect
- Our causal forest: 4000 trees using 50% of sample, 50% honesty
 - Outcome var: financial structure, assets, and payout policy; treatment: downgrade
 - Covariates: SecDebt, UnsecDebt, Debt, NetInc, MktCap, Div (all /Assets); SecDebt/Debt; Rating; MktCap; Assets; Tangibility

Causal Forest – Treatment Effect Densities

Density of conditional avg. treatment effects (CATEs)

- Treatment: ratings downgrades by one notch (or more)
- Effect on secured debt leverage and secured debt ratio
- Densities for treatment effects on the treated (TT) and control (TC)



Estimates of average treatment effects • ATE/ATT/ATC

Causal Forest – Heterogenous Treatment Effects

Treatment effect of one-notch (or more) downgrade by rating



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Secured Debt (Lease-adj.)

Conclusion

Secured debt enables higher leverage but entails costs

- Explicit collateralization gives secured lender strong claim on assets
- More constrained firms use more secured debt within and across firms

Collateral restricts both secured and unsecured debt

- Unsecured debt backed by unencumbered assets
- Consistent with stylized facts and evidence from causal forest

Collateral is essential to understanding capital structure

- Collateral constraints matter despite large firms borrowing unsecured
- Firms shift to secured debt when constrained
- Bulk of debt secured for small firms and lease-adj. for most firms
- Unsecured debt implicitly collateralized

Assets and dividend payout across rating deciles



- Firms with low ratings are smaller and pay lower (or no) dividends
 - Low rated firms seem more constrained



Within-firm variation: Assets & payout effect of downgrades



Downgraded firms downsize and reduce payout substantially



Assets and dividend payout across size deciles



Dramatic size pattern in dividends



Stylized Fact 1 – Secured Debt and Leasing



Panel A: Secured debt/Assets (lease-adj.) F



Panel C: Leasing debt/Assets (lease-adj.)



Panel D: Debt/Assets (lease-adj.)



Cross section: accentuated patterns and higher level

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Stylized Fact 1 - Secured Debt and Leasing

Within-firm variation: heterogeneous effects of downgrades

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Panel A: Secured debt/Assets (lease-adj.)

Panel C: Leasing debt/Assets (lease-adj.)

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Panel B: Secured debt/Total debt (lease-adj.)

Firms that are downgraded shift to secured debt and leasing

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Previous rating decile

Collateral and Secured Debt

Stylized Fact 1 – Secured Debt and Leasing

Shift to secured debt (incl. leasing), esp. low-rated firms



Stylized Fact 1 – Secured Debt and Leasing

Financial structure and leasing across size deciles



Panel C: Leasing debt/Assets (lease-adj.)



Panel B: Secured debt/Total debt (lease-adj.)



Panel D: Debt/Assets (lease-adj.)



Bulk of financing secured in all but largest firms

Stylized Fact 2 – Financial Structure and Tangible Assets

Financial structure and leasing across tangibility deciles



Panel C: Leasing debt/Assets (lease-adj.)

3 4 5 6 7 8 Tangible assets ratio (lease-adj.) deciles

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Panel B: Secured debt/Total debt (lease-adj.)



Secured debt, leasing, and total leverage all increase with tangibility

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Stylized Facts – Secured LT Debt Ratio (Lease-Adj.)

Ratio of secured debt to long-term debt (lease-adj.)





Panel C: Δ Secured LT debt ratio



Panel B: Secured LT debt ratio by assets



Panel D: Secured LT debt ratio by tangibility



Patterns in secured LT debt still more pronounced

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Collateral and Secured Debt

Model with Secured and Unsecured Debt and Leasing

• Benefits and costs of leasing k_l

- Monitoring cost m > 0; leasing fee $\wp_l \equiv R^{-1}u + m$
- Assumption 5. $R^{-1}(1-\theta_s)(1-\delta) > m-\kappa > \frac{1-\theta_s}{\theta_s-\theta_u}\kappa$
- Implies $\wp_s > \wp_l$ and $R_l \equiv \frac{(1-\theta_s)(1-\delta)}{\wp_s (R^{-1}u+m)} > R_s$
- Repossession advantage: Eisfeldt/Rampini (2009); R/V (2013)

Firm's problem

$$v(w,z) = \max_{\{d,k_s,k_u,k_l,w',b'_s,b'_u\} \in \mathbb{R}^5_+ \times \mathbb{R}^{2S}} d + \beta E[v(w',z')|z]$$
(18)

subject to budget constraints for current and next period, $\forall z' \in Z$,

$$w + E\Big[\sum_{j \in \mathcal{J}} b'_j \Big| z\Big] \ge d + \frac{1}{\varphi} \sum_{j \in \mathcal{J}} k_j + \kappa k_s + \frac{1 - \varphi + \varphi(R^{-1}u + m)}{\varphi} k_l$$
$$A'f\Big(\frac{1}{\varphi}\Big(\sum_{j \in \mathcal{J}} k_j + k_l\Big)\Big) + \frac{1}{\varphi}\Big(\sum_{j \in \mathcal{J}} k_j + (1 - \varphi)k_l\Big)(1 - \delta) \ge w' + \sum_{j \in \mathcal{J}} Rb'_j$$

and collateral constraints (4) $\forall \{j,z'\} \in \mathcal{J} \times Z$

Prediction: Most constrained firms lease, then borrow secured < Back</p>

Average Treatment Effects from Causal Forest

- Effects on financial structure, investment, and payout policy
- ATE/ATT/ATC: Average Treatment Effect; on Treated; on Control

Outcome variable	ATE	ATT	ATC
Secured debt /Assets	0.021	0.016	0.022
	(6.973)	(5.602)	(6.962)
Secured debt/Total debt	0.032	0.025	0.033
	(5.629)	(4.914)	(5.563)
Unsecured debt/Assets	0.018	0.011	0.019
	(4.753)	(3.230)	(4.829)
Debt/Assets	0.040	0.027	0.042
	(9.740)	(7.340)	(9.803)
Log assets (level)	-0.101	-0.110	-0.099
	(-8.746)	(-11.220)	(-8.222)
Dividends/Assets	-0.004	-0.003	-0.004
	(-11.329)	(-12.098)	(-10.998)

Causal Forest – Treatment Effects (Lease-adj.)

Treatment effect of one-notch (or more) downgrade by rating



Secured debt/Assets (lease-adj.)

Secured debt/Total debt (lease-adj.)



Average Treatment Effects from Causal Forest

Treatment Effects on Financial Structure (Lease-adj.)

Outcome variable	ATE	ATT	ATC
Secured debt /Assets	0.024	0.020	0.025
	(8.753)	(7.415)	(8.719)
Secured debt/Total debt	0.016	0.019	0.015
	(3.464)	(4.453)	(3.236)
Unsecured debt/Assets	0.012	0.005	0.013
	(3.956)	(1.559)	(4.186)
Debt/Assets	0.038	0.026	0.040
	(10.620)	(8.059)	(10.703)
Leasing debt/Assets	0.014	0.016	0.014
	(7.677)	(9.153)	(7.328)



Causal Forest – Heterogenous Treatment Effects

Treatment effect of one-notch (or more) downgrade by rating





▲ Back

Causal Forest – Heterogenous Treatment Effects

Assets

Treatment effect of one-notch (or more) downgrade by rating



Dividends/Assets



Causal Forest – Treatment Effects (Lease-adj.)

Treatment effect of one-notch (or more) downgrade by rating



Unsecured debt/Assets (lease-adj.)



