

# **ECE/CS 250**

## **Computer Architecture**

### **Summer 2019**

#### Basics of Logic Design: Storage Elements and the Register File (Sequential Logic)

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Duke University

Slides are derived from work by  
Daniel J. Sorin (Duke), Alvy Lebeck (Duke), and Drew Hilton (Duke)

# So far...

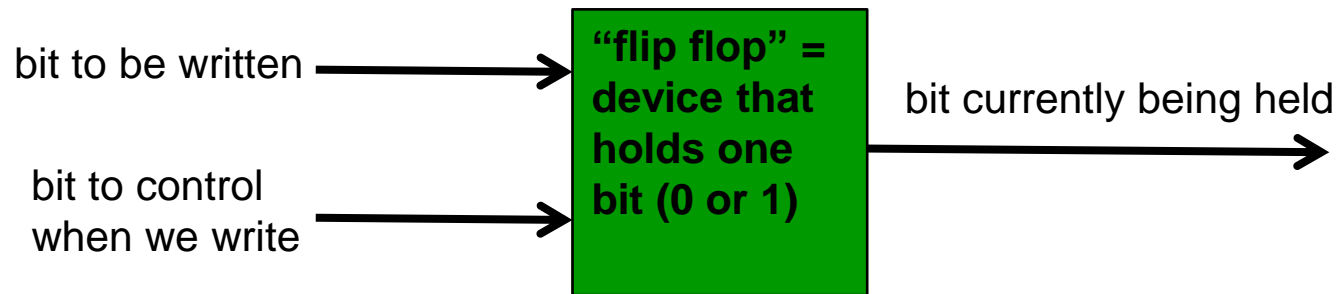
- We can make logic to compute “math”
  - Add, subtract ... and you can do mul/div in 350
    - Assume for now that mul/div can be built
  - Bitwise: AND, OR, NOT,...
  - Shifts (left or right)
  - Selection (MUX)
  - ...pretty much anything
- But processors need state (hold value)
  - Registers
  - ...

# Storage

- All the circuits we looked at so far are **combinational circuits**: the output is a Boolean function of the inputs.
- We need circuits that can remember values (registers, memory)
- The output of the circuit is a function of the input and a function of a stored value (state)
- Circuits with storage are called **sequential circuits**
- Key to storage: feedback loops from outputs to inputs

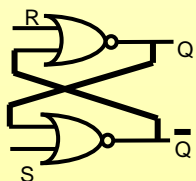
# Ideal Storage – Where We're Headed

- Ultimately, we want something that can hold 1 bit and we want to control when it is re-written



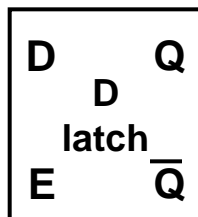
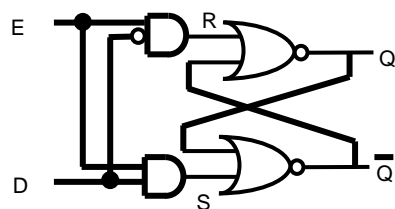
- However, instead of just giving it to you as a magic black box, we're going to first dig a bit into the box
  - I will not test you on the insides of the “flip flop”

# Building up to the D Flip-Flop and beyond



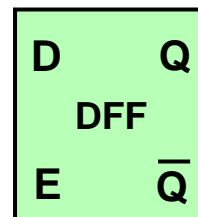
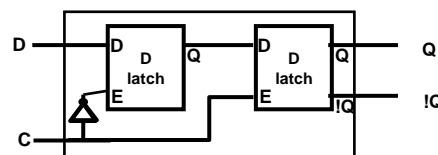
SR Latch

(too awkward)



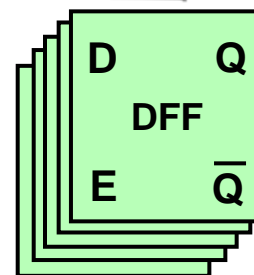
D Latch

(bad timing)



D Flip-Flop

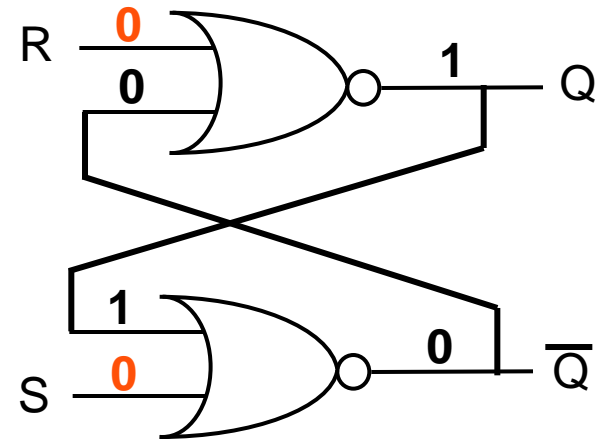
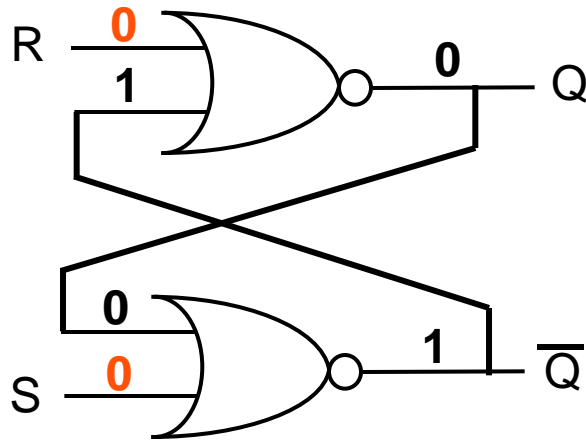
(okay but only one bit)



Register

(nice!)

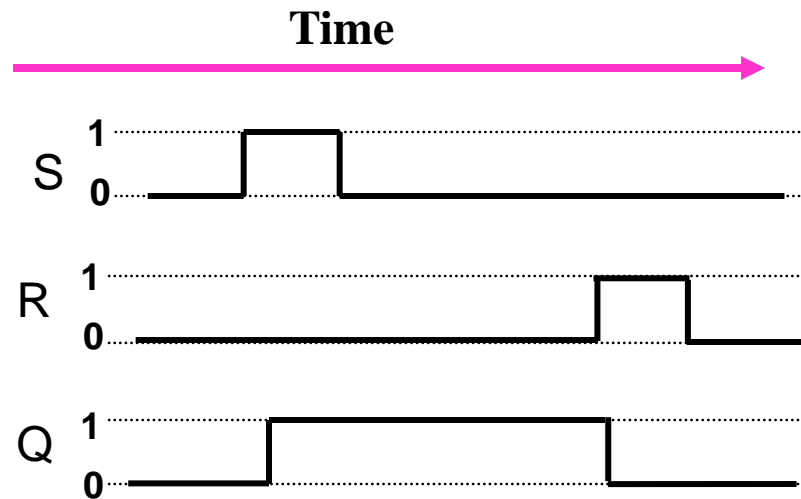
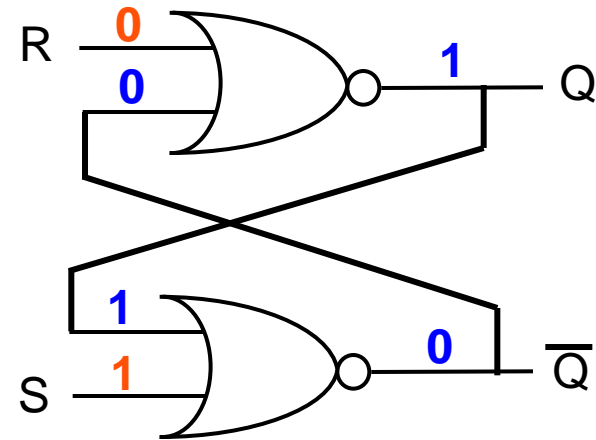
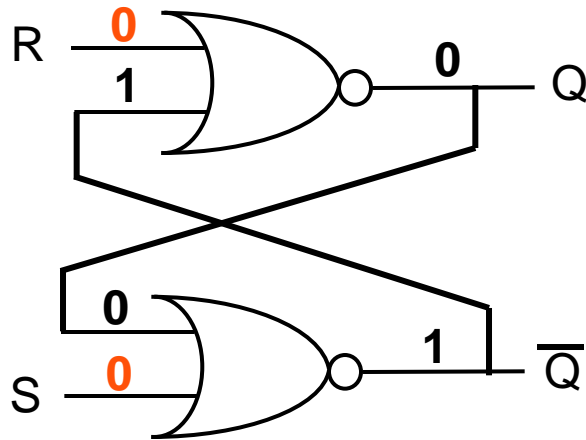
# FF Step #1: NOR-based Set-Reset (SR) Latch



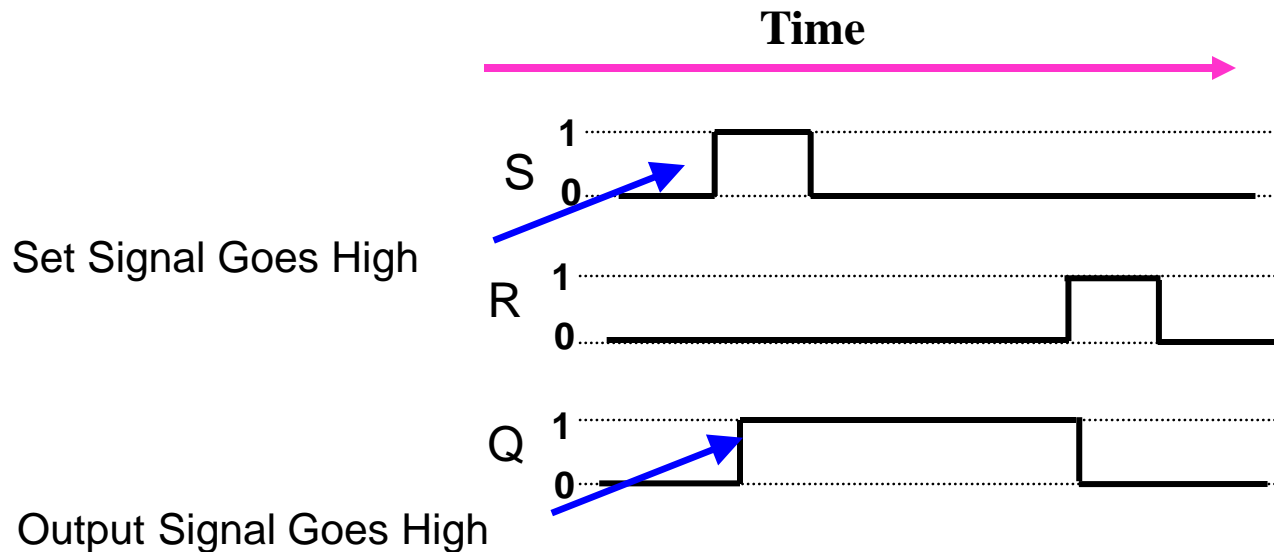
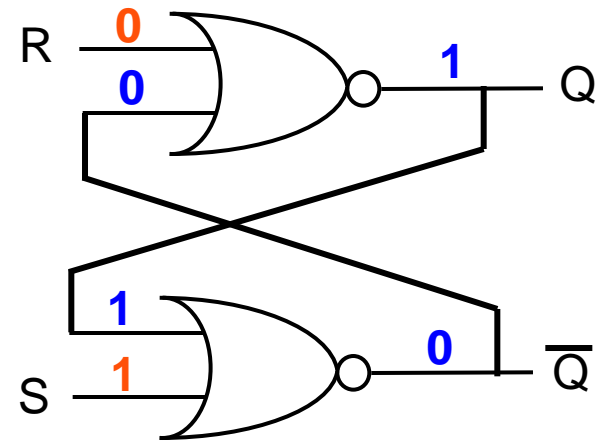
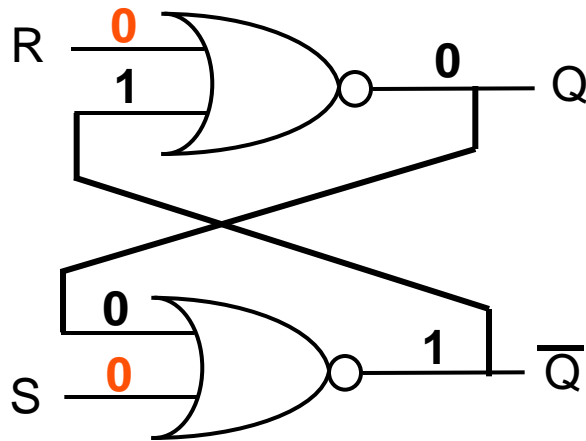
R	S	Q
0	0	Q
0	1	1
1	0	0
1	1	—

Don't set both S & R to 1.  
Seriously, don't do it.

# Set-Reset Latch (Continued)

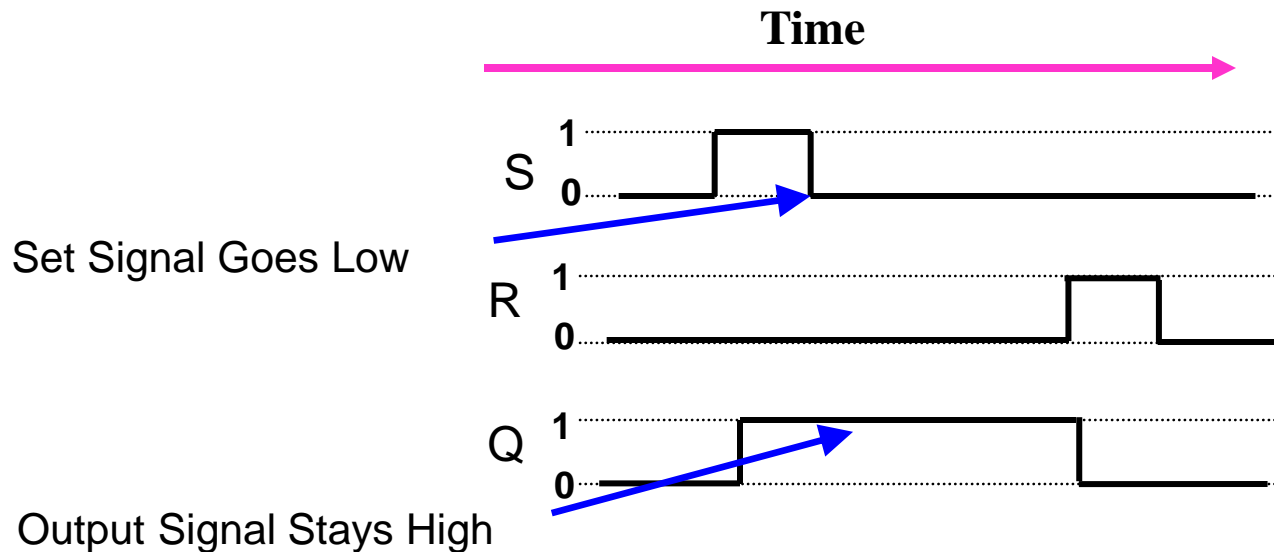
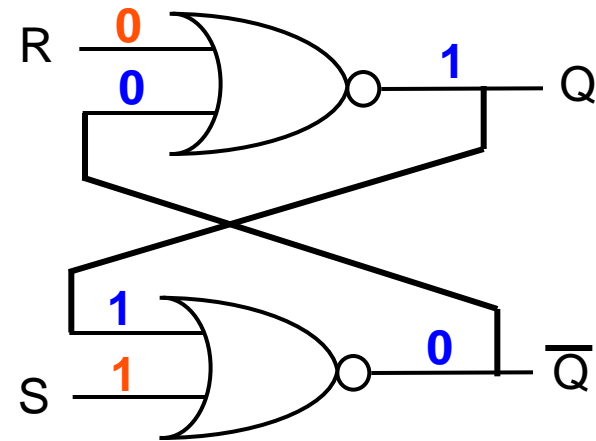
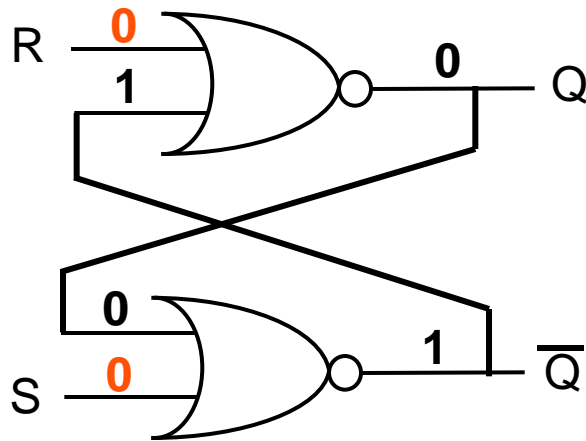


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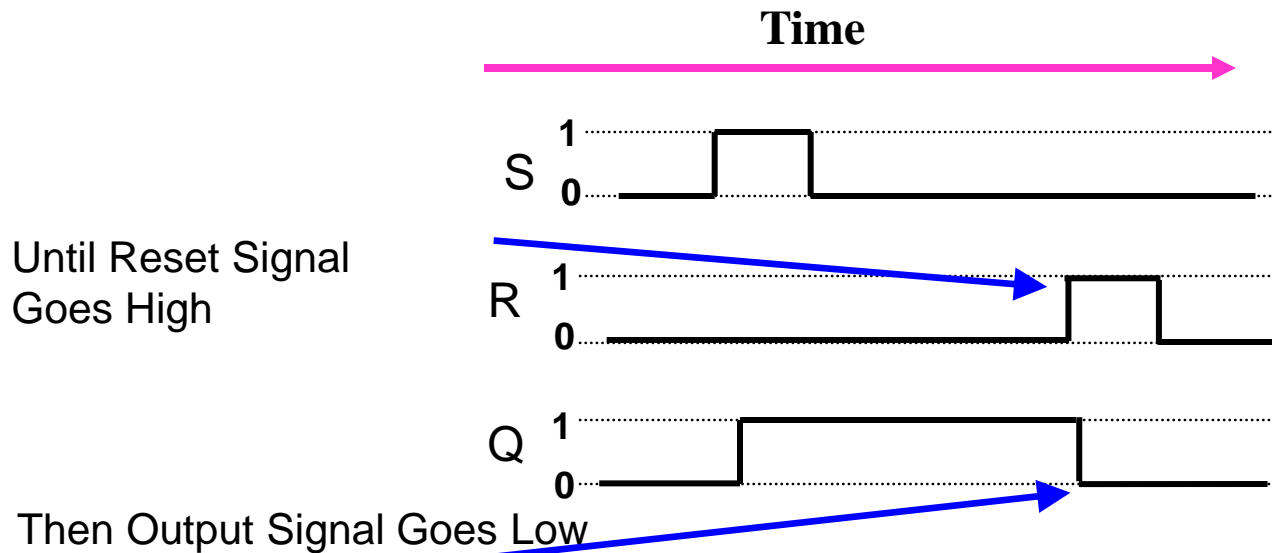
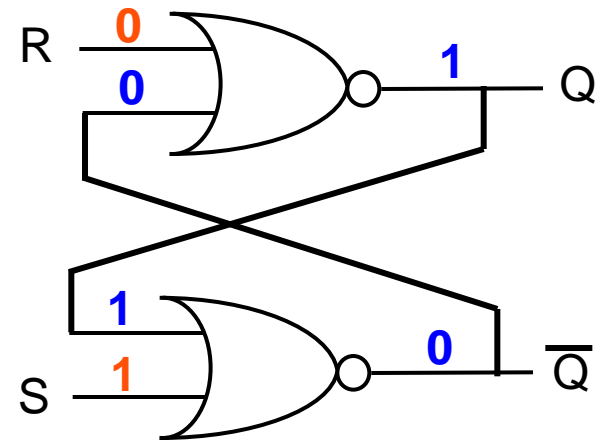
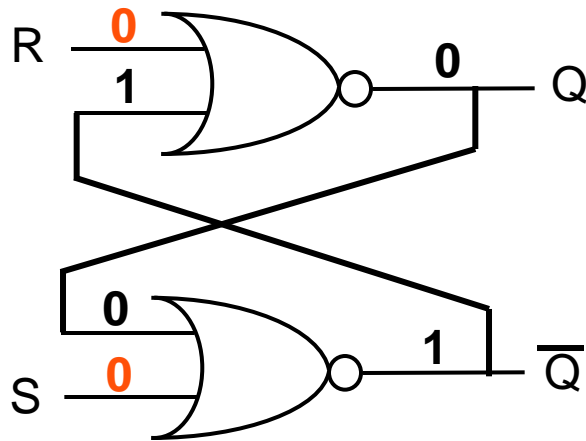




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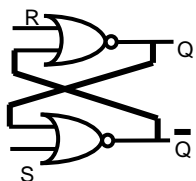
# Set-Reset Latch (Continued)



# SR Latch

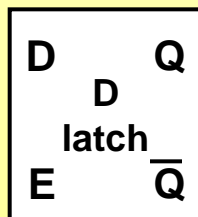
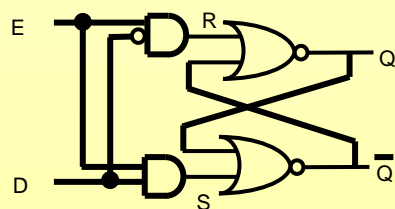
- Downside: S and R at once = chaos
- Downside: Bad interface
- So let's build on it to do better

# Building up to the D Flip-Flop and beyond



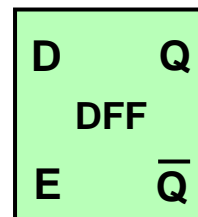
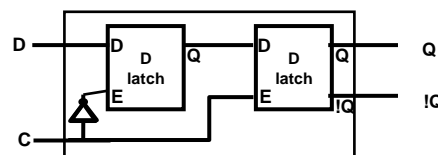
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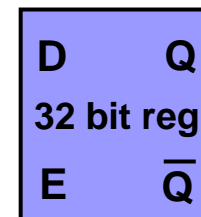
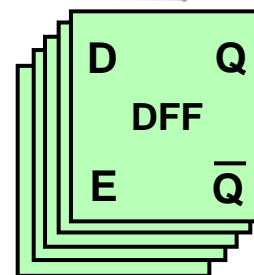
D Latch

(bad timing)



D Flip-Flop

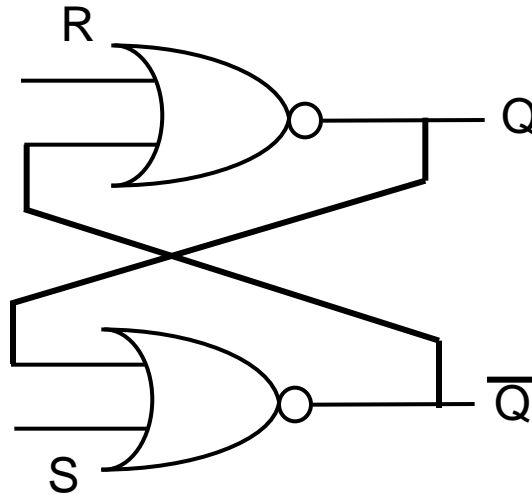
(okay but only one bit)



Register

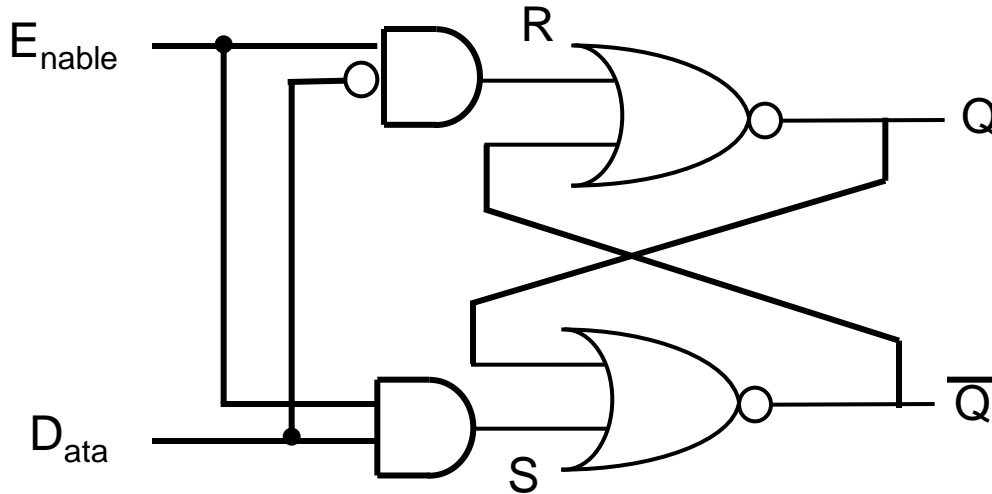
(nice!)

## FF Step #2: Data Latch (“D Latch”)



Starting with SR Latch

# Data Latch (D Latch)



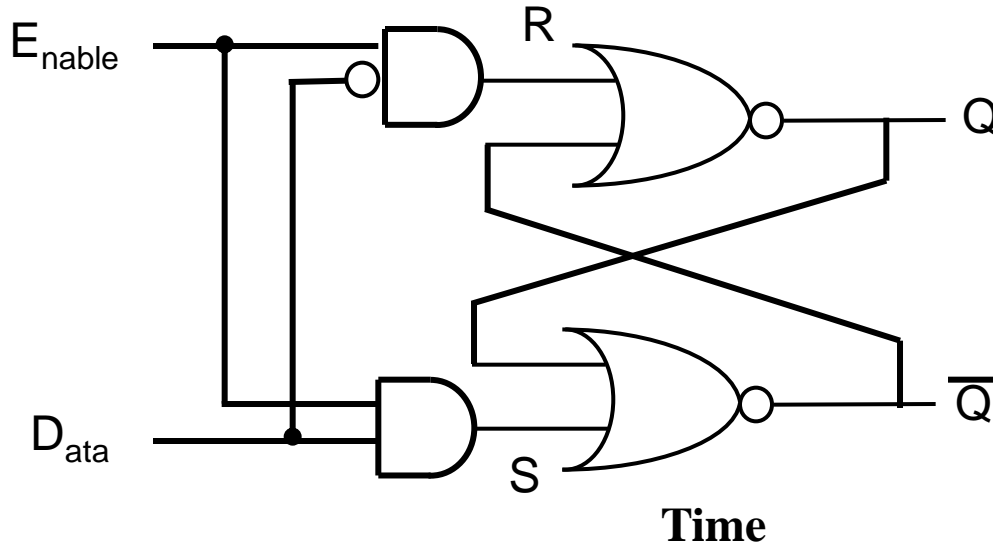
Starting with SR Latch

Change interface to  
Data + Enable ( $D + E$ )

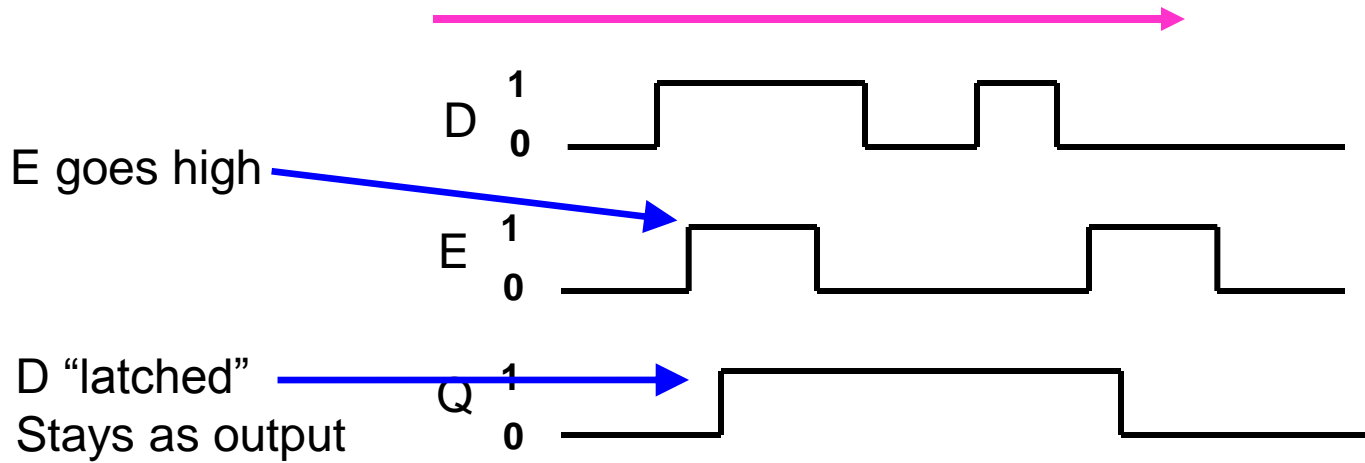
If  $E=0$ , then  $R=S=0$ .

If  $E=1$ , then  $S=D$  and  $R=\neg D$

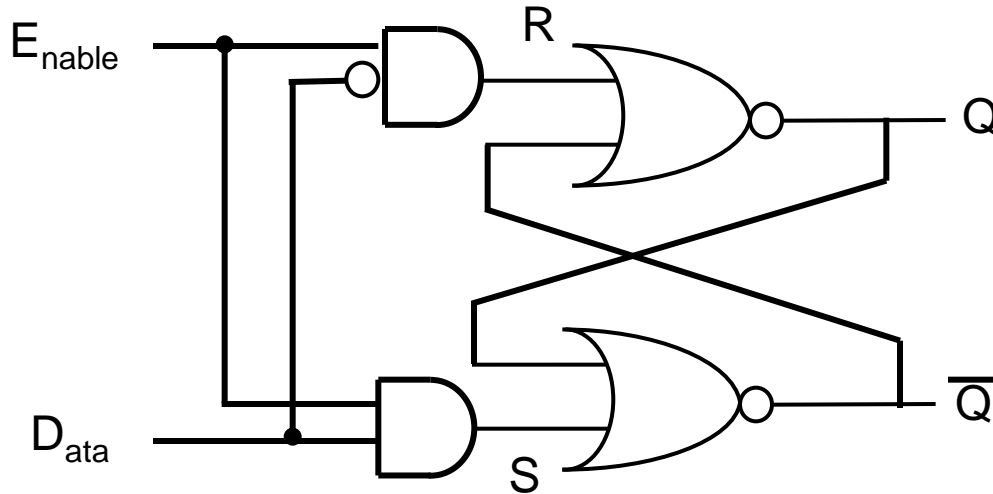
# Data Latch (D Latch)



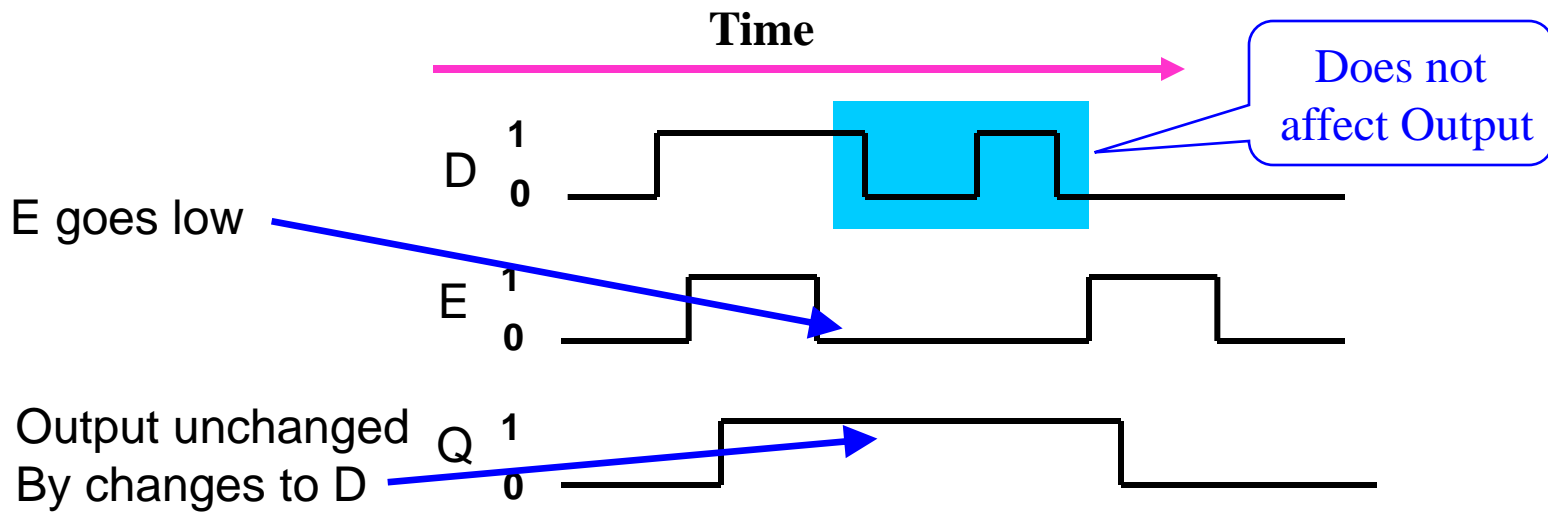
D	E	Q
0	1	0
1	1	1
-	0	Q



# Data Latch (D Latch)

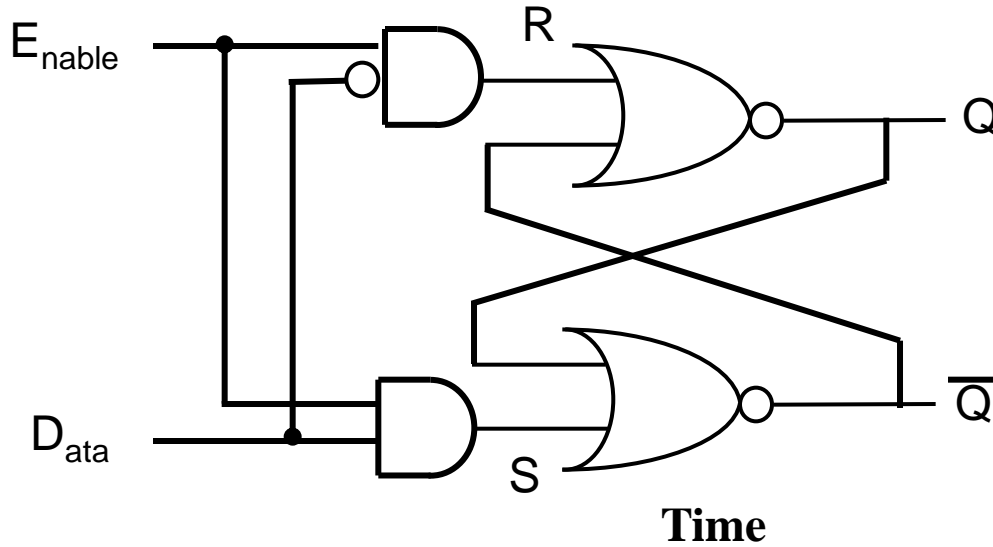


D	E	Q
0	1	0
1	1	1
-	0	Q

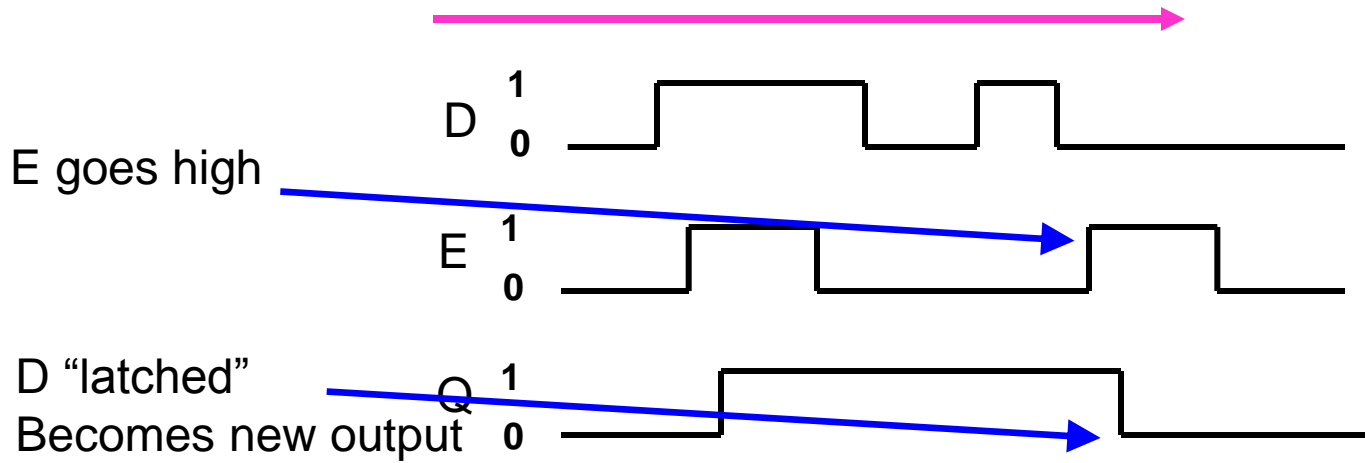




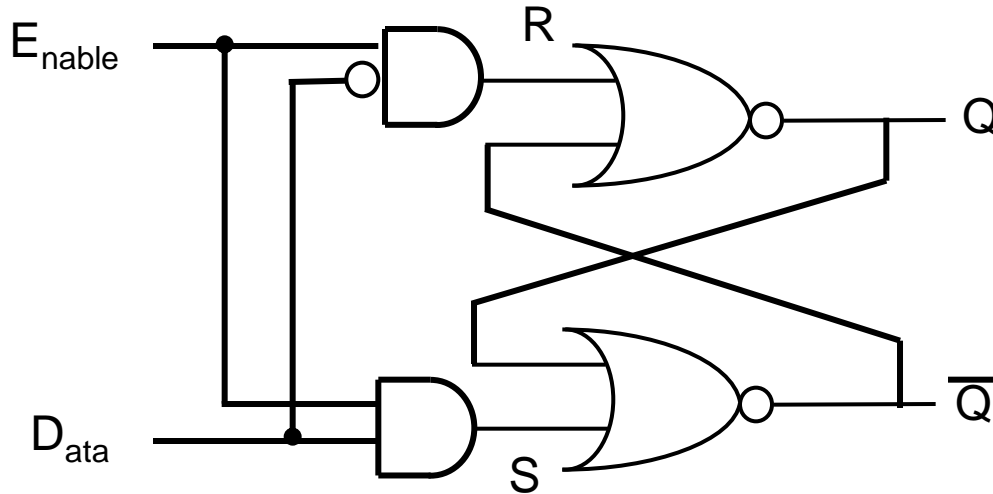
# Data Latch (D Latch)



D	E	Q
0	1	0
1	1	1
-	0	Q

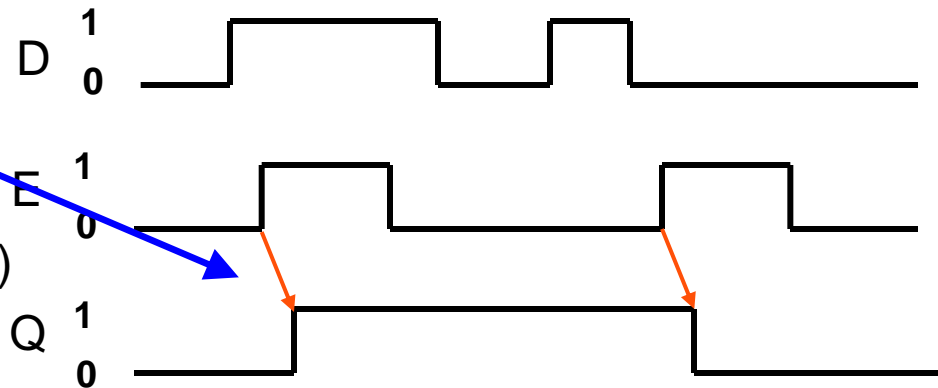


# Data Latch (D Latch)



D	E	Q
0	1	0
1	1	1
-	0	Q

Time →



Slight Delay

(Logic gates take time)

# Logic Takes Time

- Logic takes time:
  - Gate delays: delay to switch each gate
  - Wire delays: delay for signal to travel down wire
  - Other factors (not going into them here)
- Need to make sure that signals timing is right
  - Don't want to have races or wacky conditions..

# Clocks

- Processors have a clock:
  - Alternates 0 1 0 1
  - Like the processor's internal metronome
  - Latch → logic → latch in one clock cycle

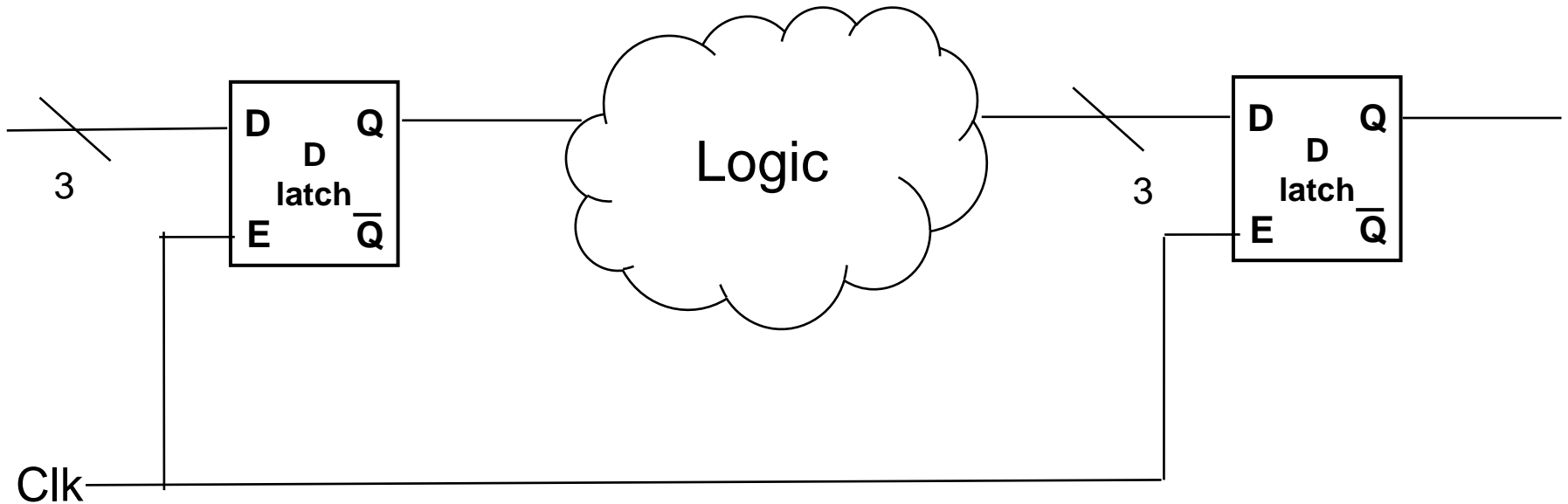


One clock cycle

- 3.4 GHz processor = 3.4 Billion clock cycles/sec

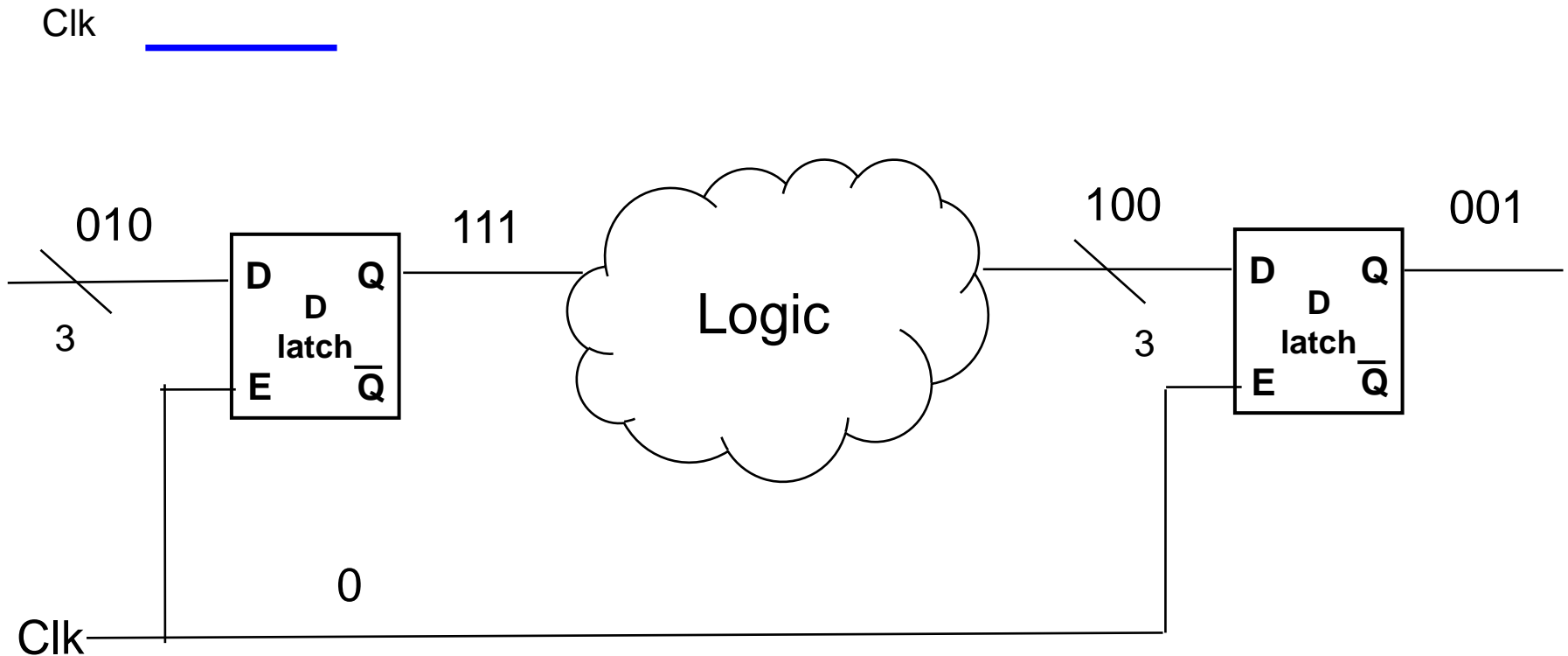
## FF Step #3: Using Level-Triggered D Latches

- First thoughts: Level Triggered
  - Latch enabled when clock is high
  - Hold value when clock is low



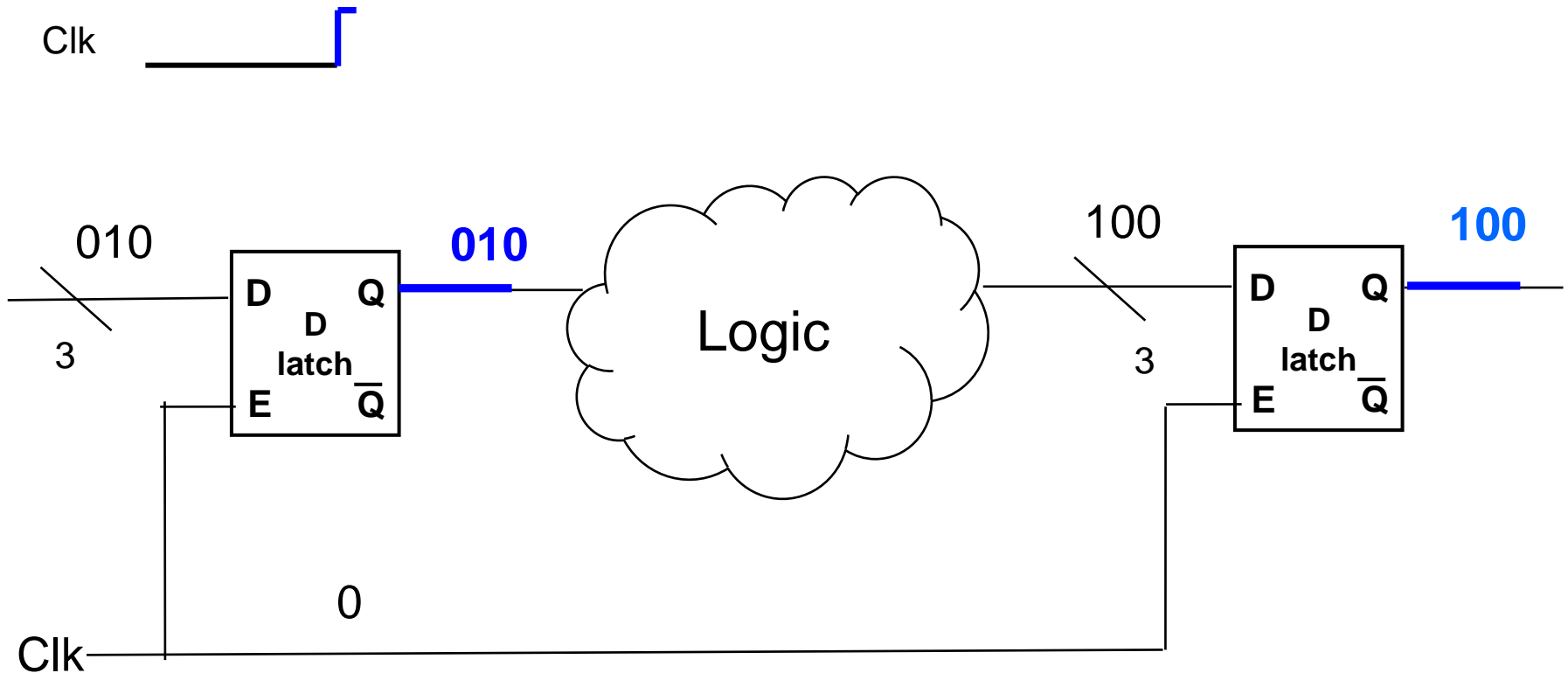
# Strawman: Level Triggered

- How we'd like this to work
  - Clock is low, all values stable



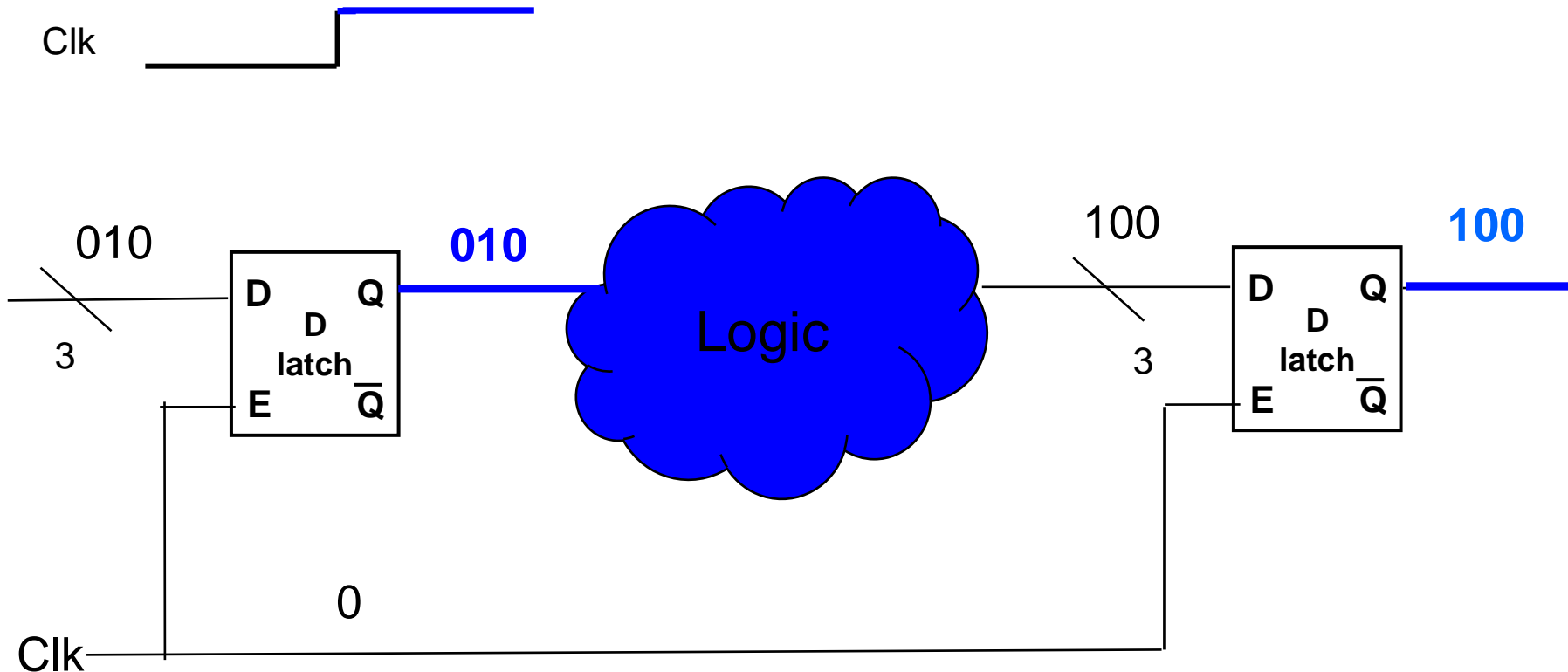
# Strawman: Level Triggered

- How we'd like this to work
  - Clock goes high, latches capture and xmit new val



# Strawman: Level Triggered

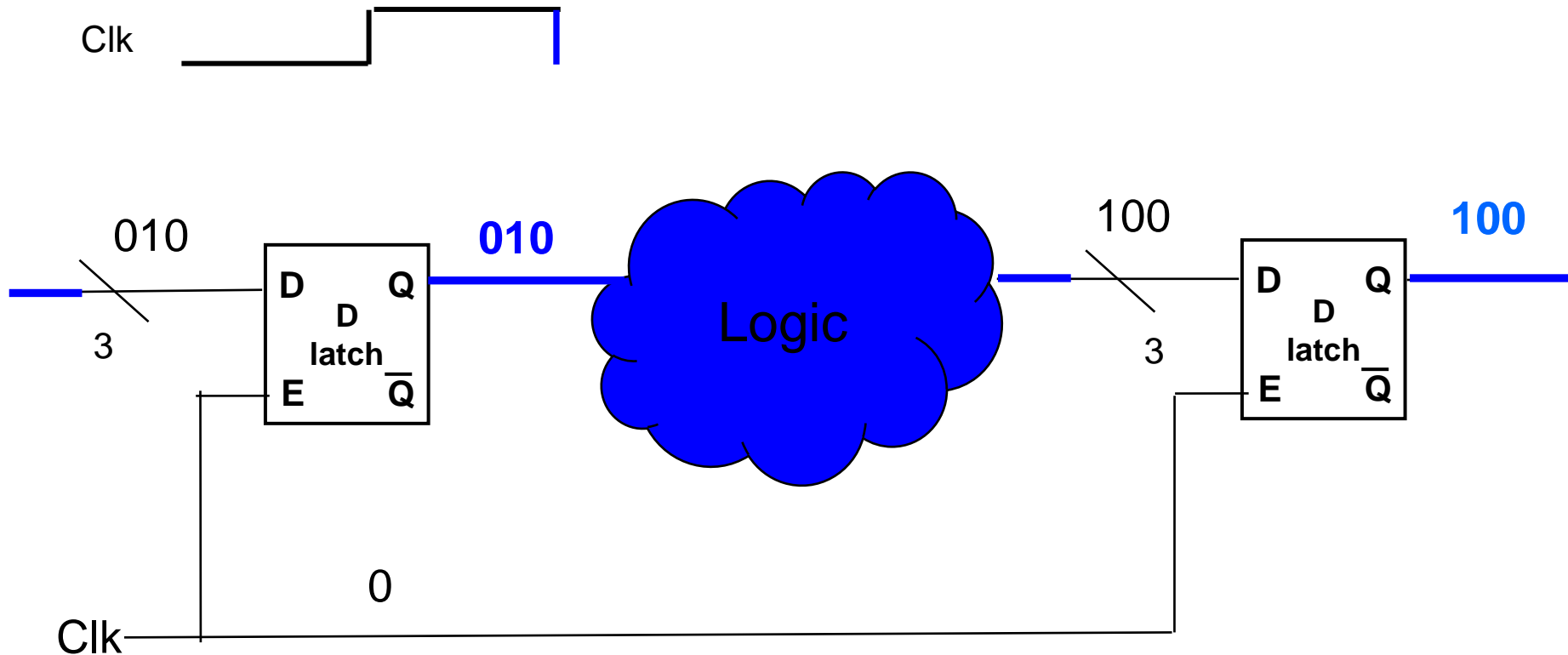
- How we'd like this to work
  - Signals work their way through logic w/ high clk





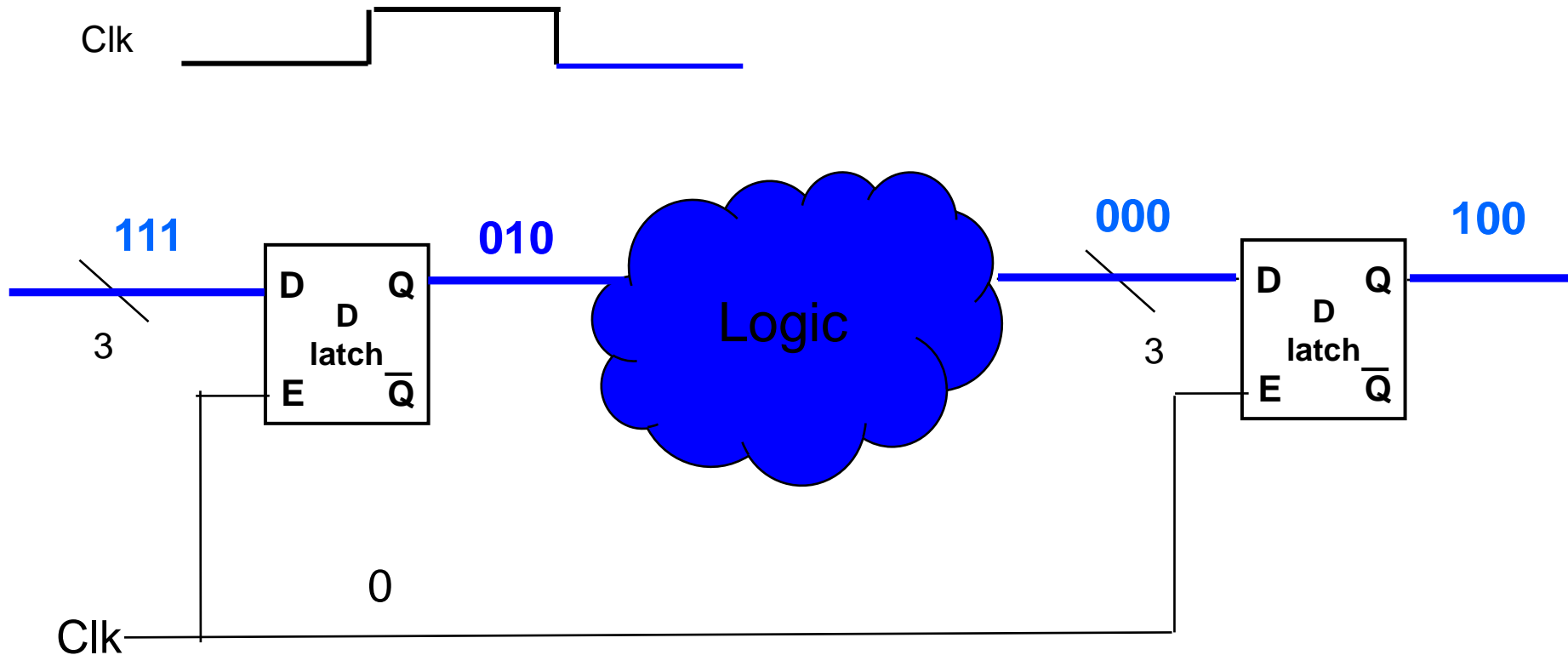
# Strawman: Level Triggered

- How we'd like this to work
  - Clock goes low before signals reach next latch



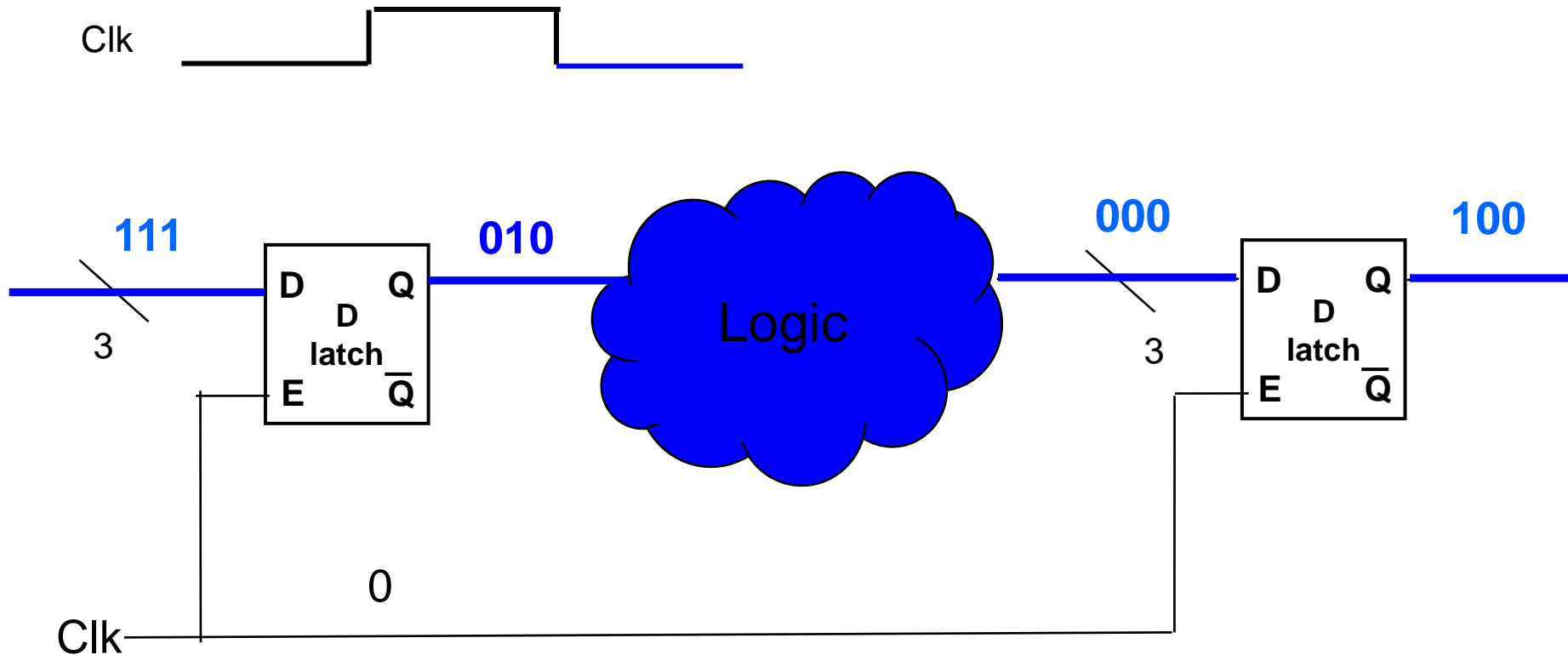
# Strawman: Level Triggered

- How we'd like this to work
  - Clock goes low before signals reach next latch



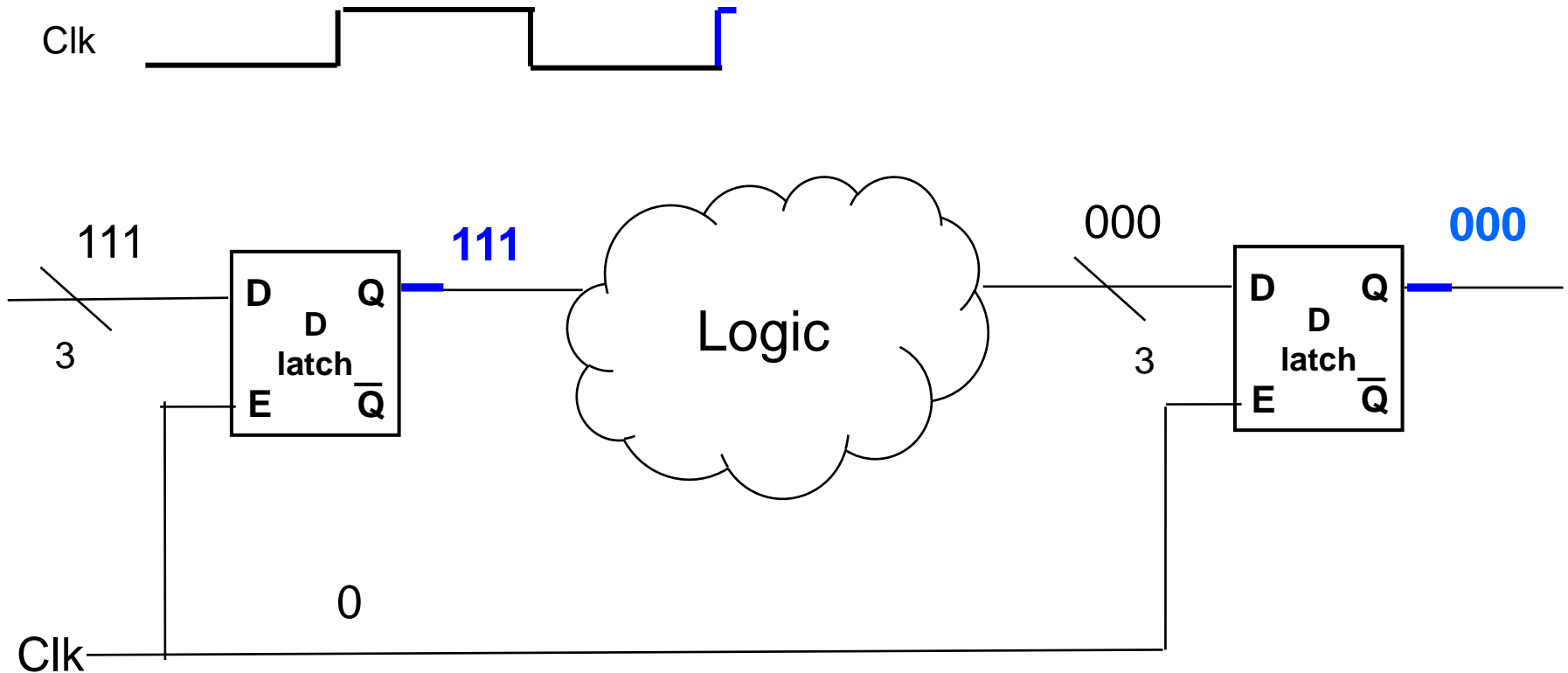
# Strawman: Level Triggered

- How we'd like this to work
  - Everything stable before clk goes high



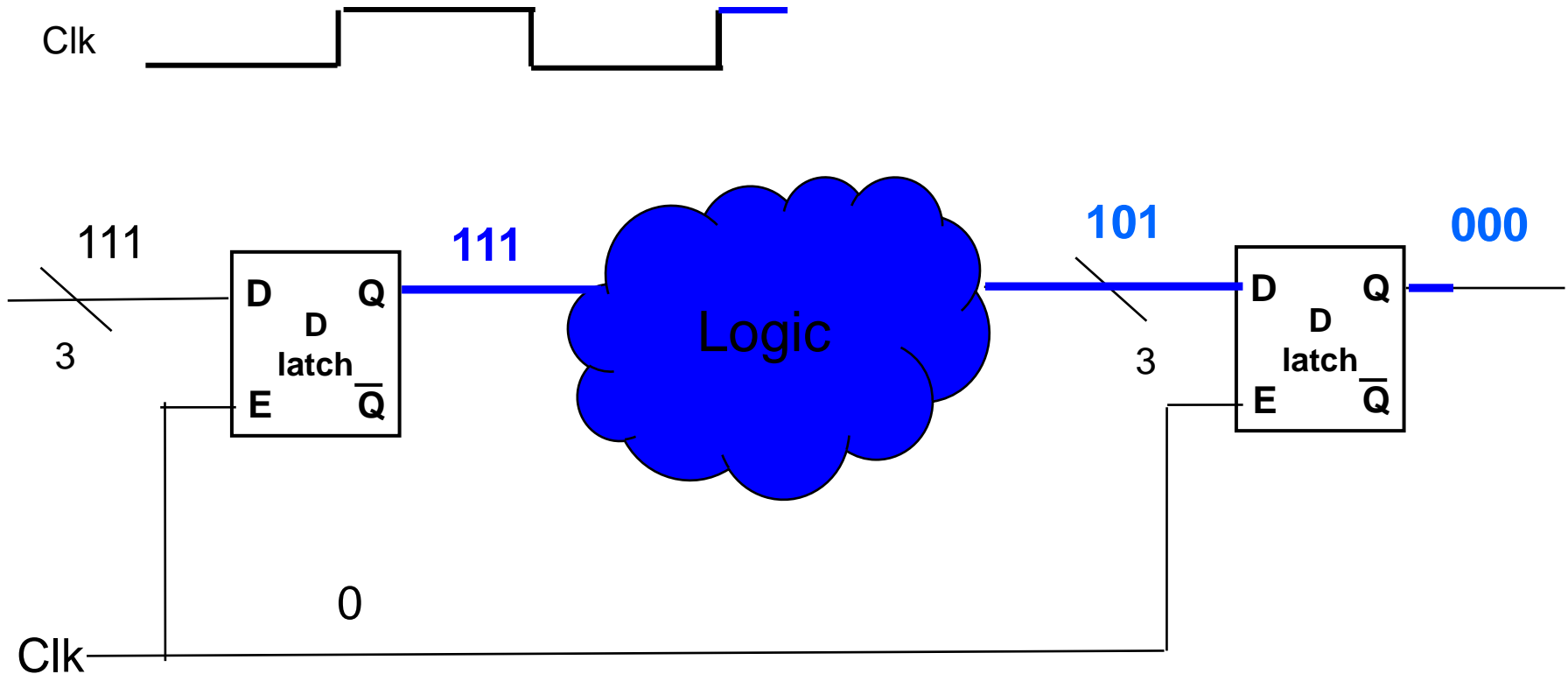
# Strawman: Level Triggered

- How we'd like this to work
  - Clk goes high again, repeat



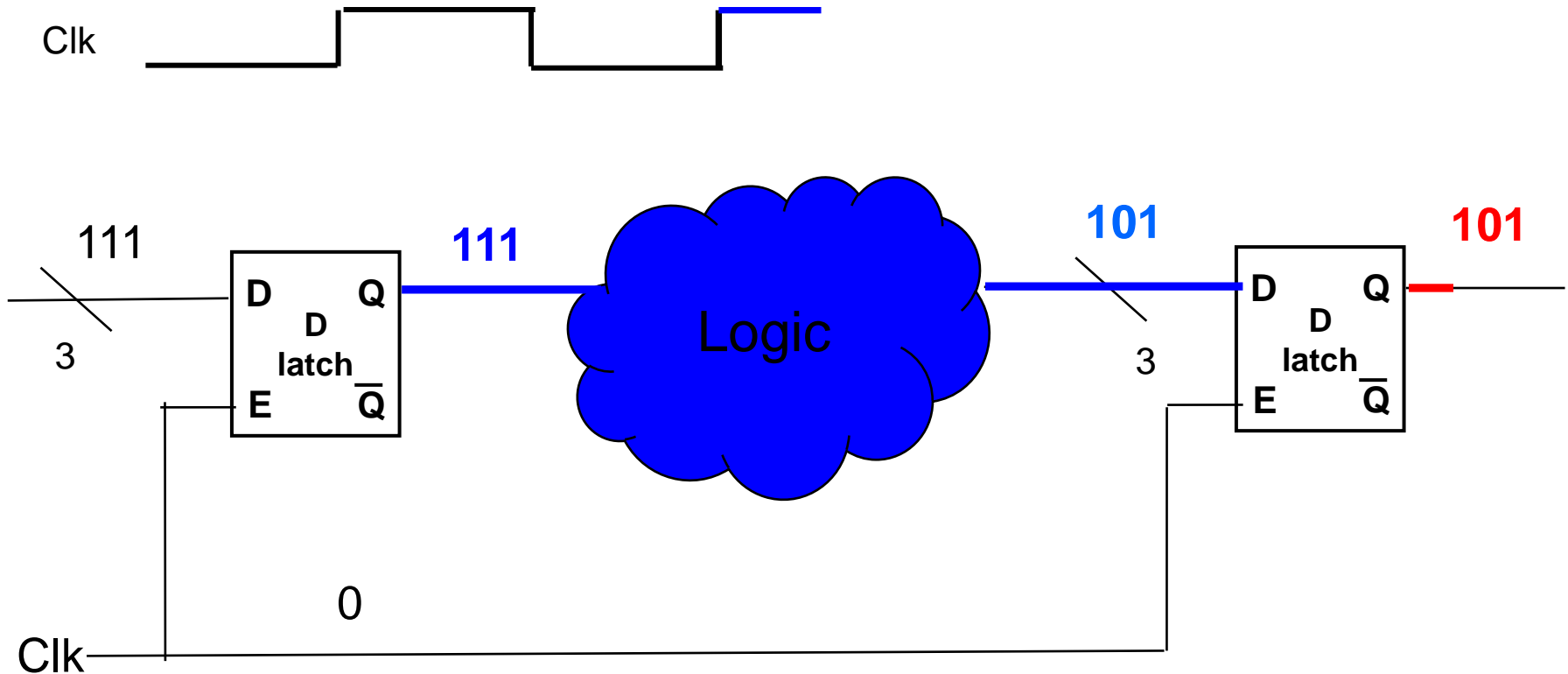
# Strawman: Level Triggered

- Problem: What if signal reaches latch too early?
  - I.e., while clk is still high



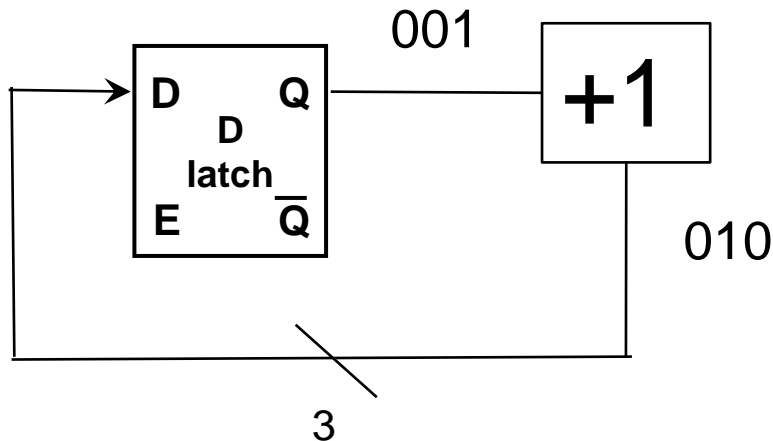
# Strawman: Level Triggered

- Problem: What if signal reaches latch too early?
  - Signal goes right through latch, into next stage..

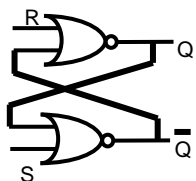


# That would be bad...

- Getting into a stage too early is bad
  - Something else is going on there → corrupted
  - Also may be a loop with one latch
- Consider incrementing counter (or PC)
  - Too fast: increment twice? Eeek...

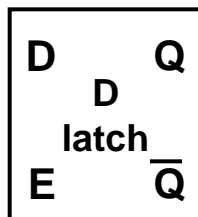
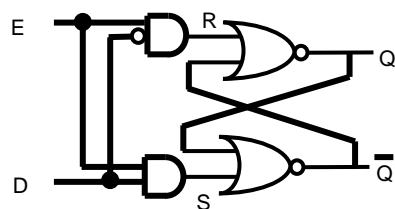


# Building up to the D Flip-Flop and beyond



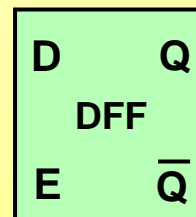
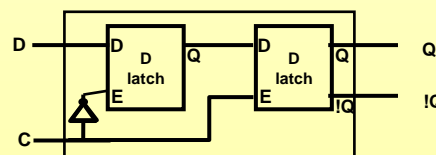
SR Latch

(too awkward)



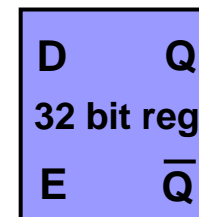
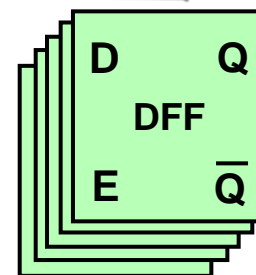
D Latch

(bad timing)



D Flip-Flop

(okay but only one bit)



Register

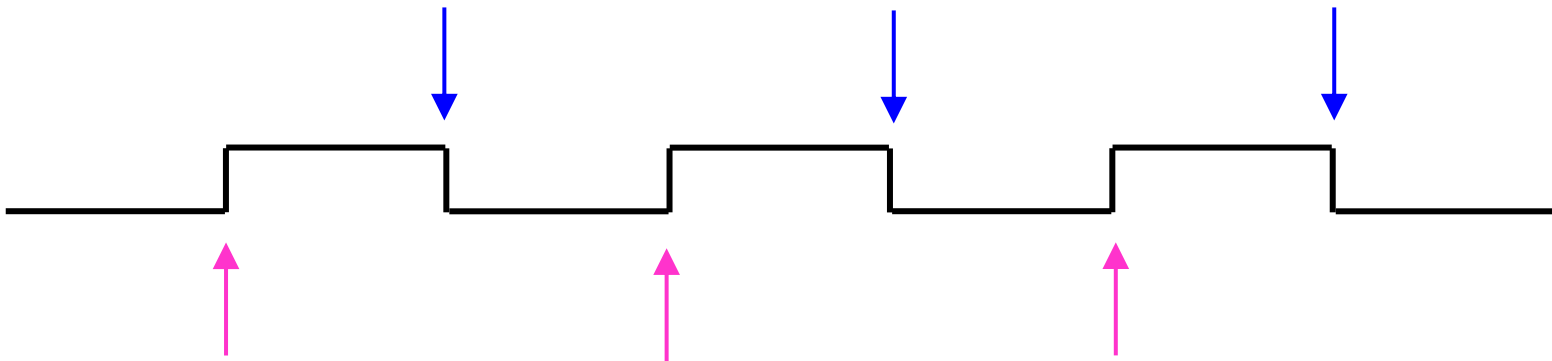
(nice!)



# FF Step #4: Edge Triggered

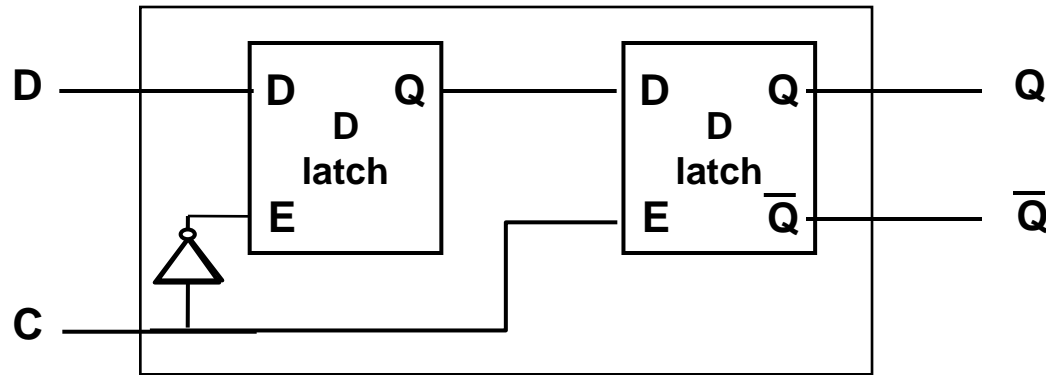
- Instead of level triggered
  - Latch a new value at a clock level (high or low)
- We use edge triggered
  - Latch a value at an clock edge (rising or falling)

**Falling Edges**



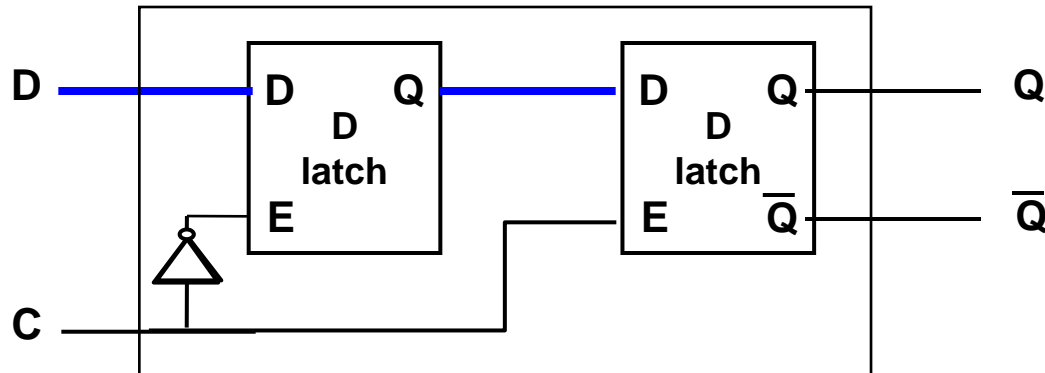
**Rising Edges**

# Our Ultimate Goal: D Flip-Flop



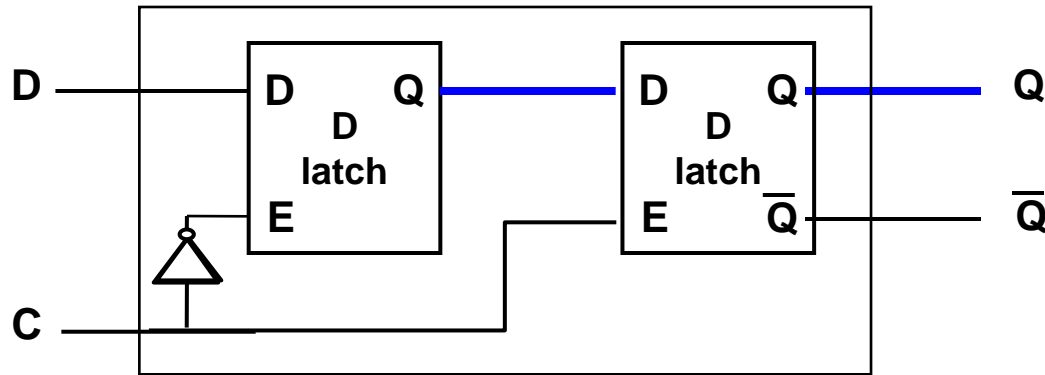
- Rising edge triggered D Flip-flop
  - Two D Latches w/ opposite clking of enables

# D Flip-Flop



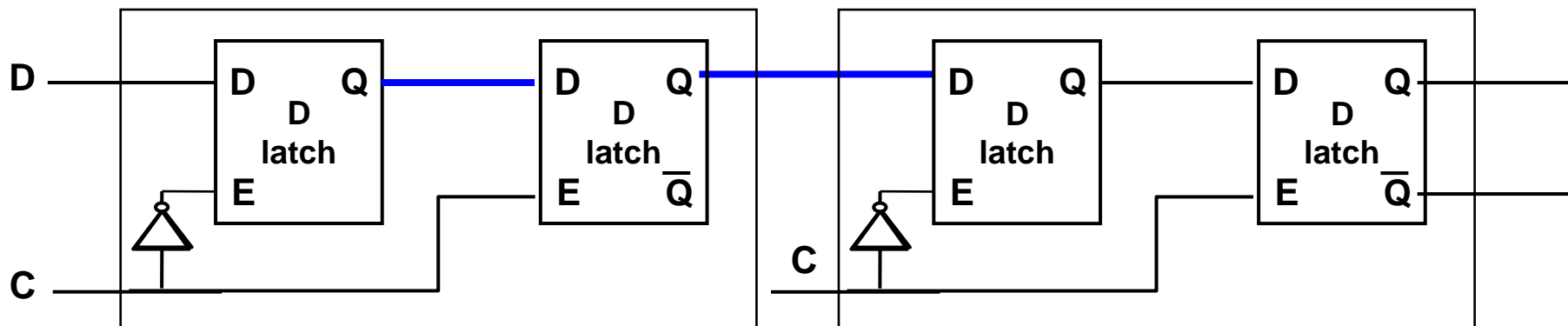
- Rising edge triggered D Flip-flop
  - Two D Latches w/ opposite clking of enables
  - On Low Clk, first latch enabled (propagates value)
    - Second not enabled, maintains value

# D Flip-Flop



- Rising edge triggered D Flip-flop
  - Two D Latches w/ opposite clking of enables
  - On Low Clk, first latch enabled (propagates value)
    - Second not enabled, maintains value
  - On High Clk, second latch enabled
    - First latch not enabled, maintains value

# D Flip-Flop



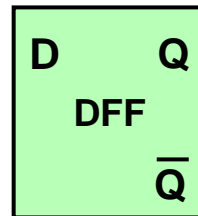
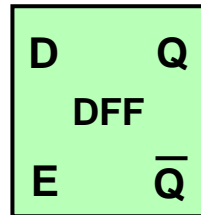
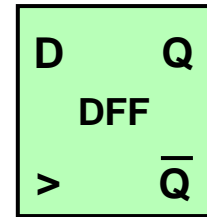
- No possibility of "races" anymore
  - Even if I put 2 DFFs back-to-back...
  - By the time signal gets through 2<sup>nd</sup> latch of 1<sup>st</sup> DFF 1<sup>st</sup> latch of 2<sup>nd</sup> DFF is disabled
- Still must ensure signals reach DFF before clk rises
  - Important concern in logic design "making timing"

# D Flip-flops (continued...)

- Could also do falling edge triggered
  - Switch which latch has NOT on clk
- D Flip-flop is ubiquitous
  - Typically people just say “latch” and mean DFF
  - Which edge: doesn't matter
    - As long as consistent in entire design
    - We'll use rising edge

# D flip flops

- Generally don't draw clk input
  - Have one global clk, assume it goes there
  - Often see > as symbol meaning clk
- Maybe have explicit enable
  - Might not want to write every cycle
  - If no enable signal shown, implies always enabled
  - Inside DFF, E signal is ANDed with Clk:  
if E is off, Clk is ignored (so we don't commit changes)



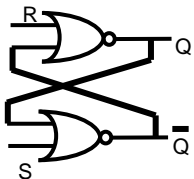
- Get output and NOT(output) for “free”

# More Storage Than A D FF: Register File

- A MIPS register can be made with 32 flip flops
- One register can store one 32-bit value
- So do we just replicate this 32 times to get the 32 registers for a MIPS processor?
  - Not exactly
- **Register File** (the physical storage for the regs)
  - MIPS register file has 32 32-bit registers
- How do we build a Register File using D Flip-Flops?
- What other components do we need?

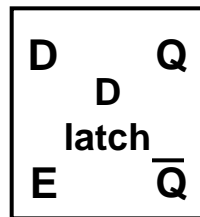
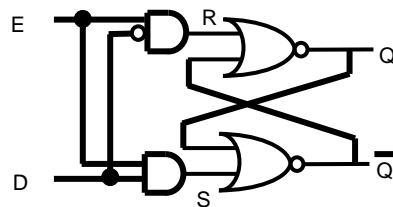


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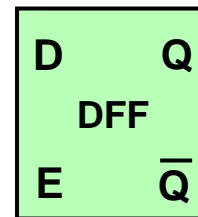
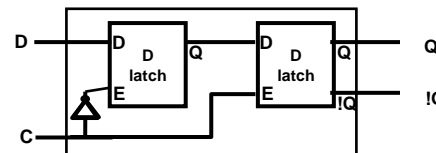
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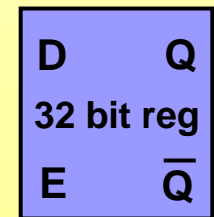
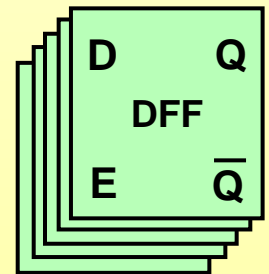
D Latch

(bad timing)



D Flip-Flop

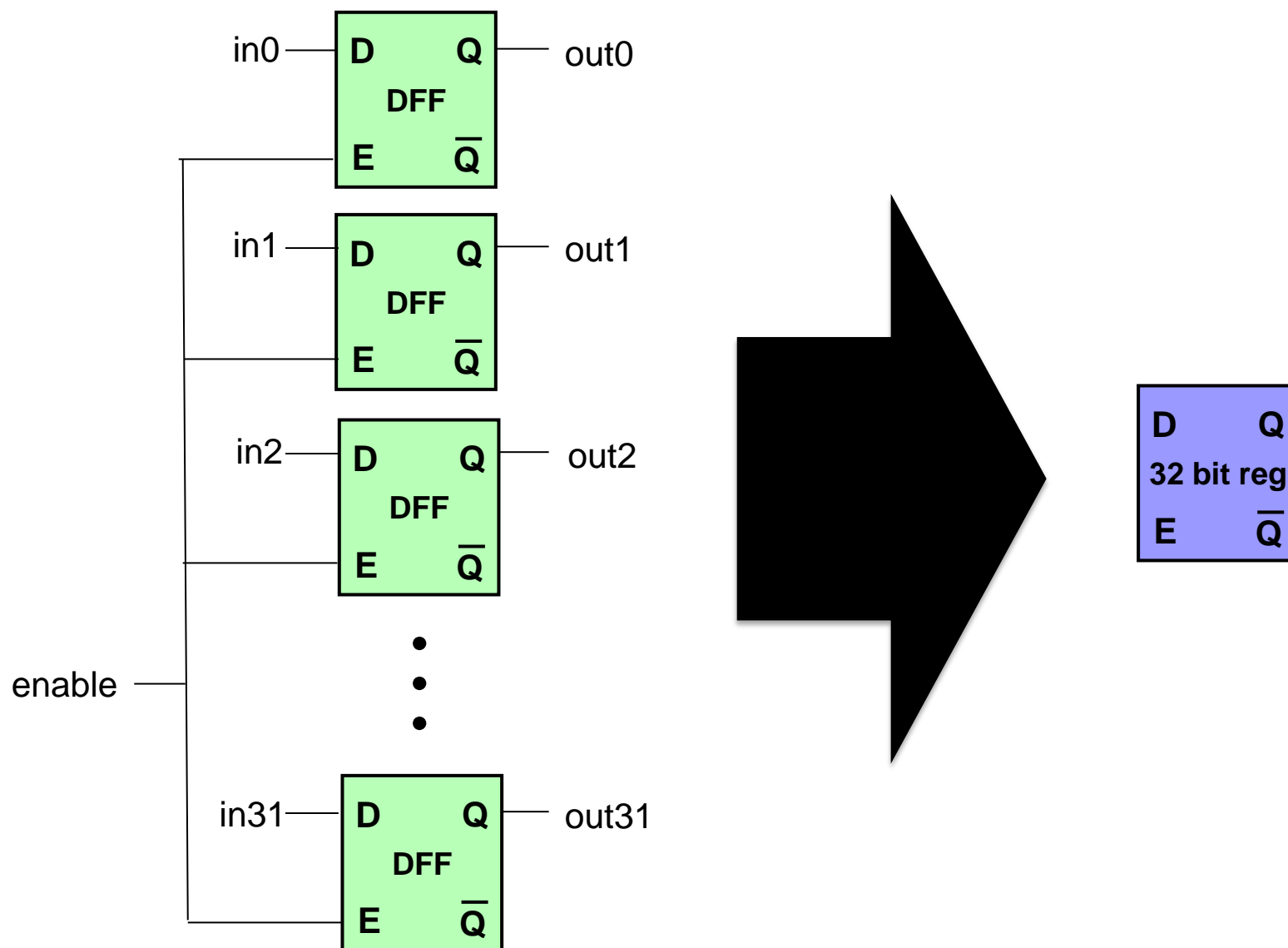
(okay but only one bit)



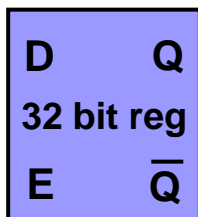
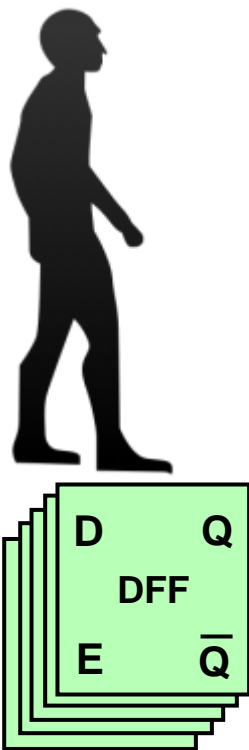
Register

(nice!)

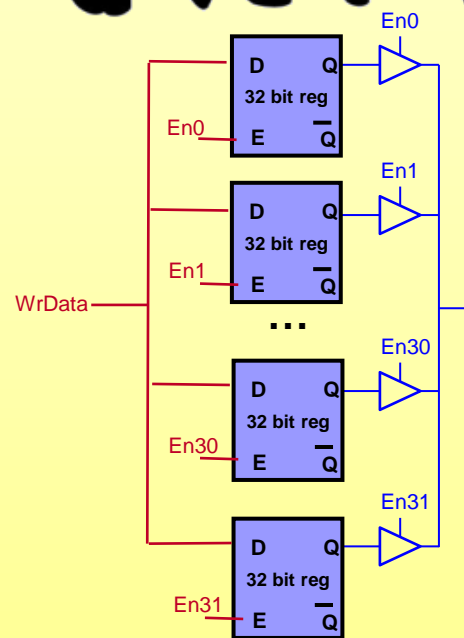
# Stick a bunch of DFFs together to make a register



# Next evolution: multiple registers



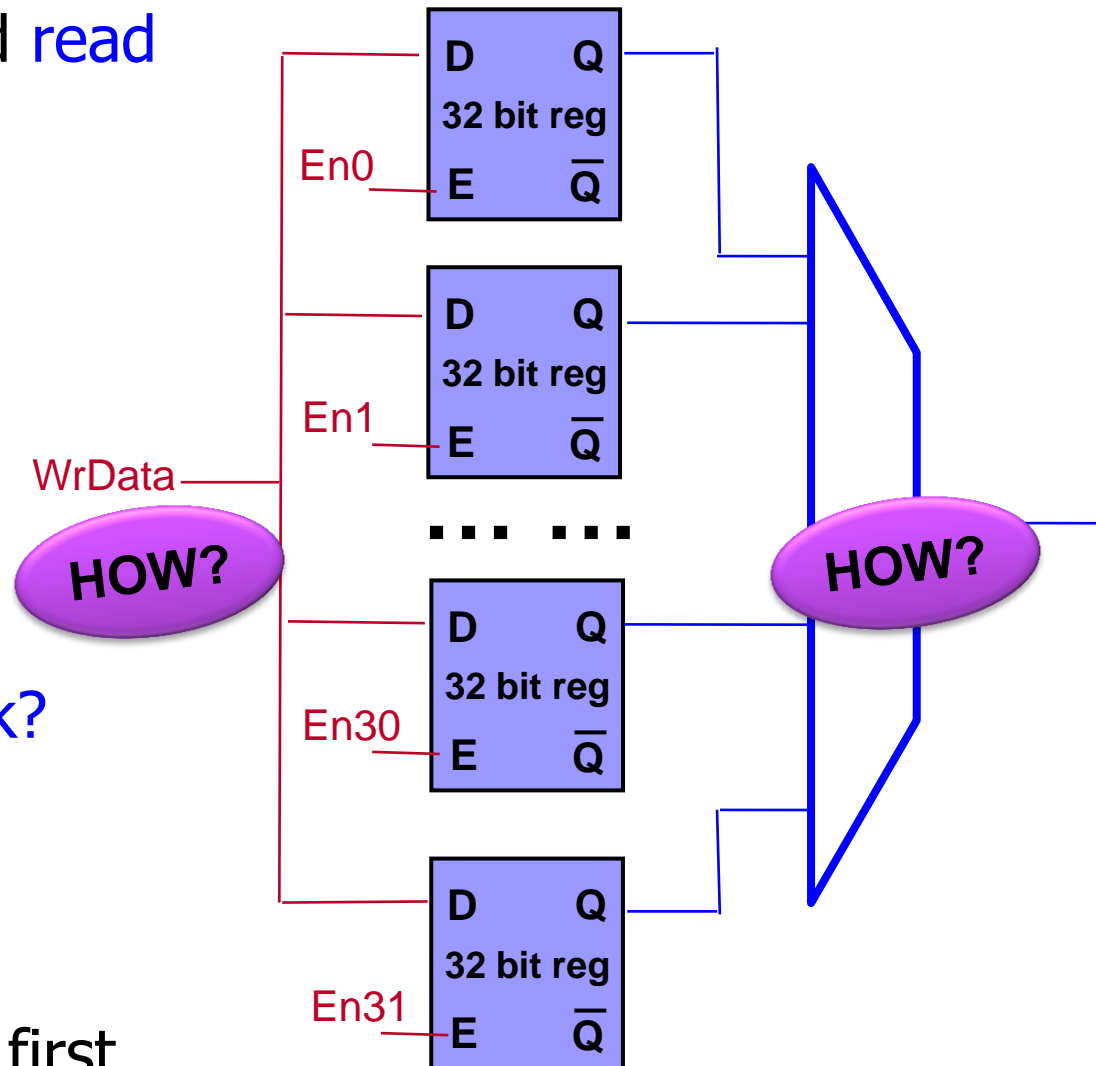
Register  
(nice!)



Register File  
(Tremendous!)

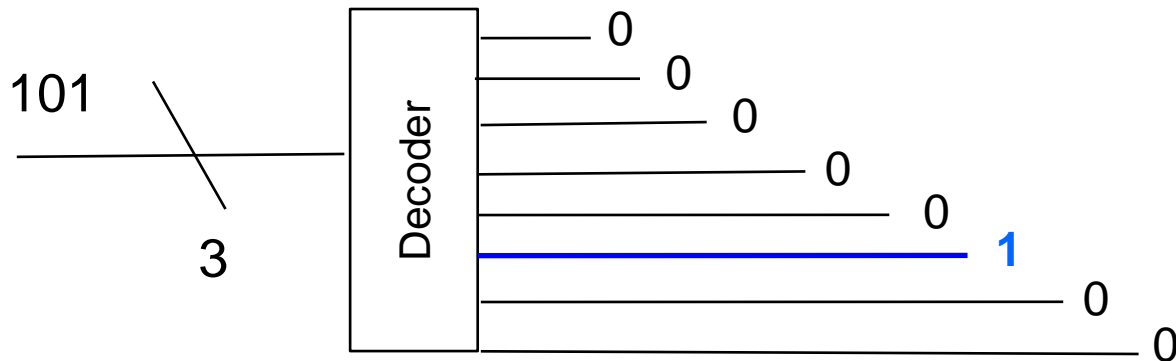
# Register File Design

- Two problems: **write** and **read**
- **Writing** the registers
  - Need to pick which reg
  - Have reg num (e.g., 19)
  - Need to make  $En_{19}=1$ 
    - $En_0, En_1, \dots = 0$
- **Read:** Use a mux to pick?
  - 32-input mux = slow
  - Need a better method...
- Let's talk about **writing** first.



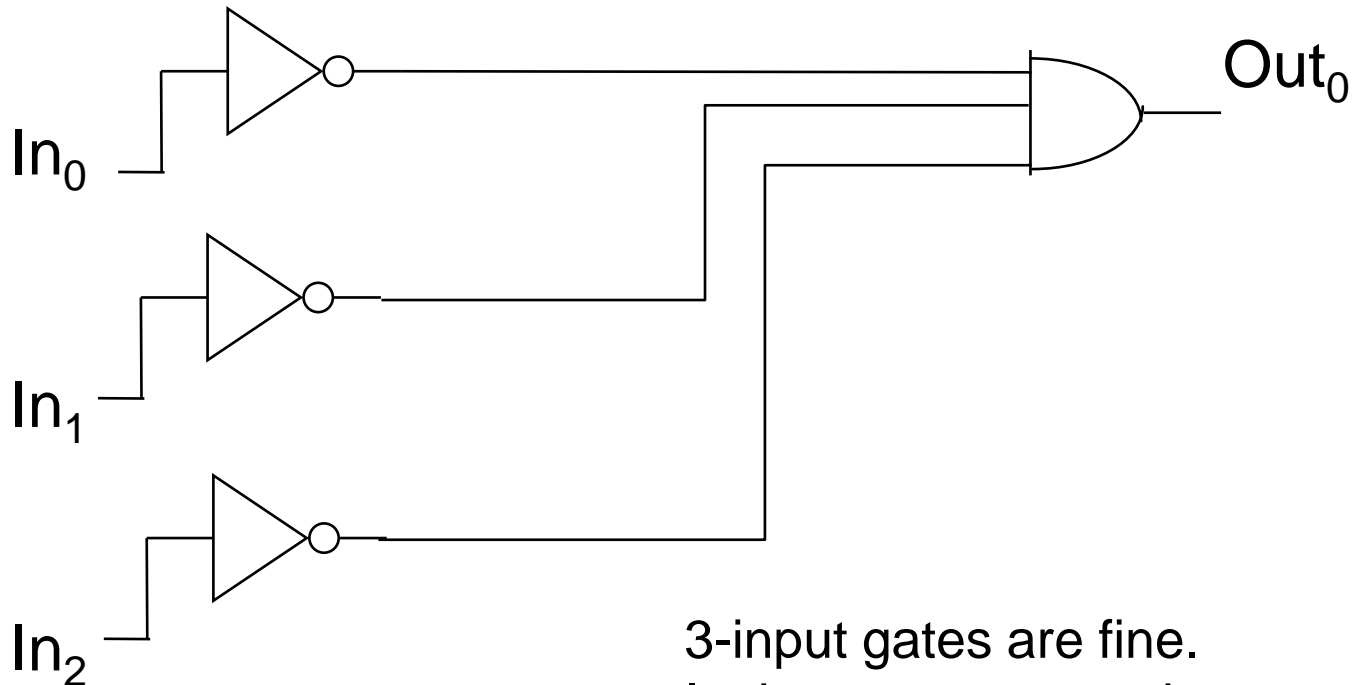
# First: A Decoder

- First task: convert binary number to “one hot”
  - N bits in
  - $2^N$  bits out
  - $2^N - 1$  bits are 0, 1 bit (matching the input) is 1



# Decoder Logic

- Decoder basically AND gates for each output:
  - $Out_0$  only on if input 000

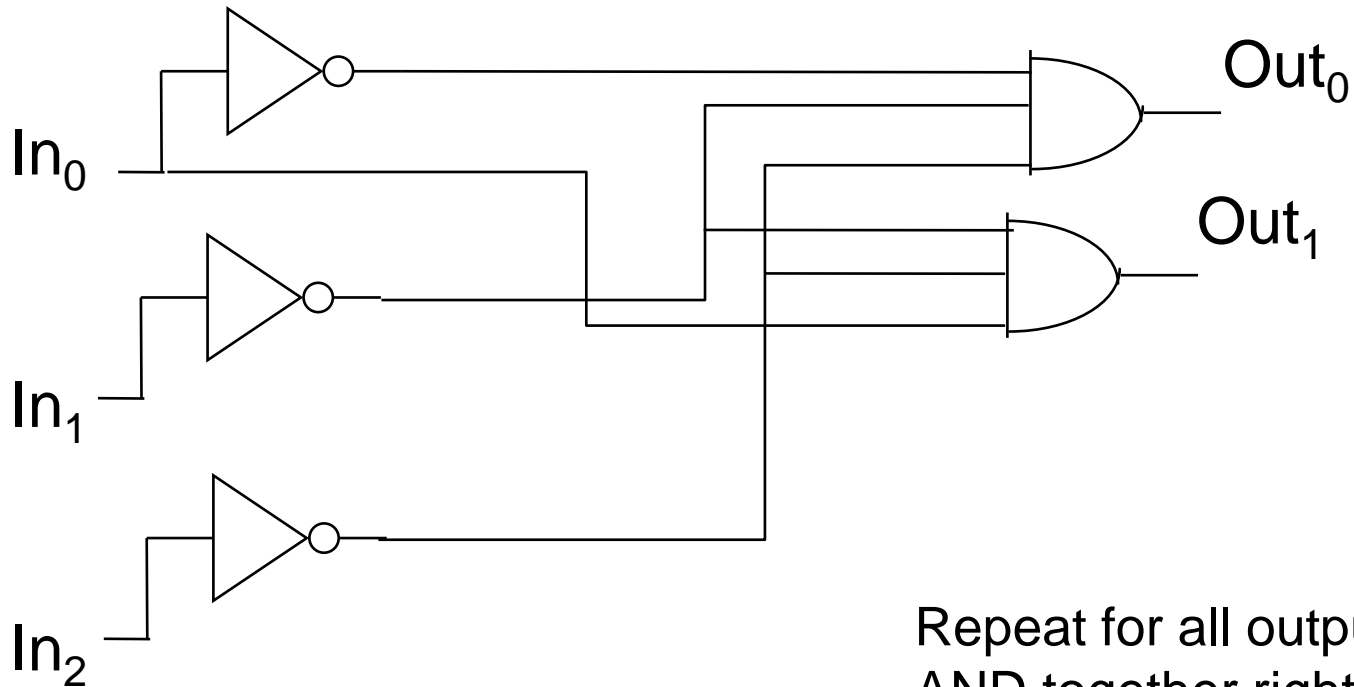


3-input gates are fine.

In theory, gates can have any # of inputs  
In practice >4 converted to multiple gates

# Decoder Logic

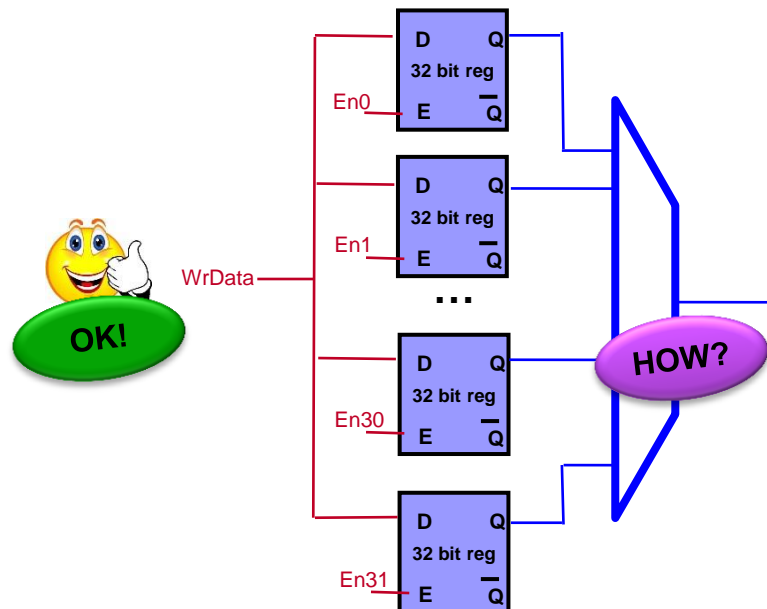
- Decoder basically AND gates for each output:
  - Out<sub>1</sub> only on if input 001



Repeat for all outputs:  
AND together right bits  
(gets messy fast on a slide)

# Register File

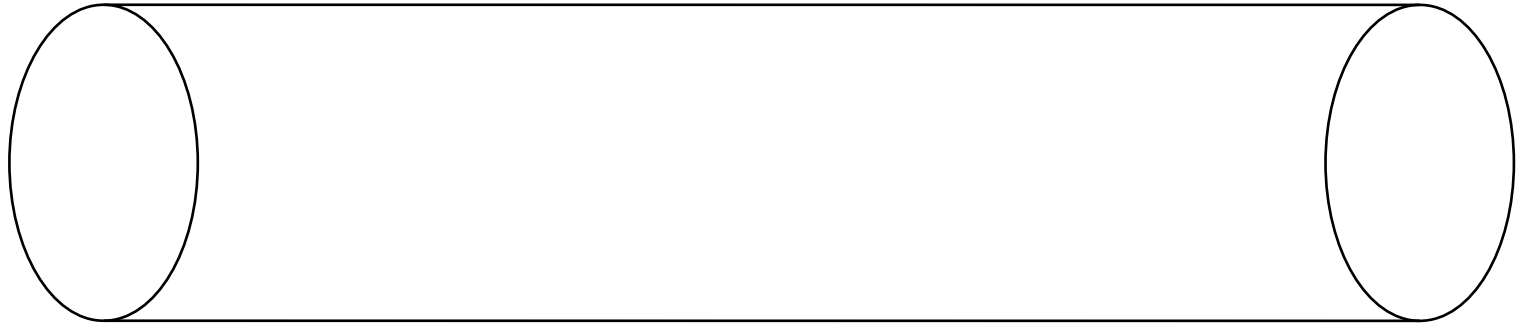
- Now we know how to **write**:
  - Use decoder to convert reg # to one hot
  - Send write data to all regs
  - Use one hot encoding of reg # to enable right reg
- Still need to fix **read** side
  - 32 input mux (the way we've made it) not realistic
  - To do this: expand our world from {1,0} to {1, 0, **Z**}





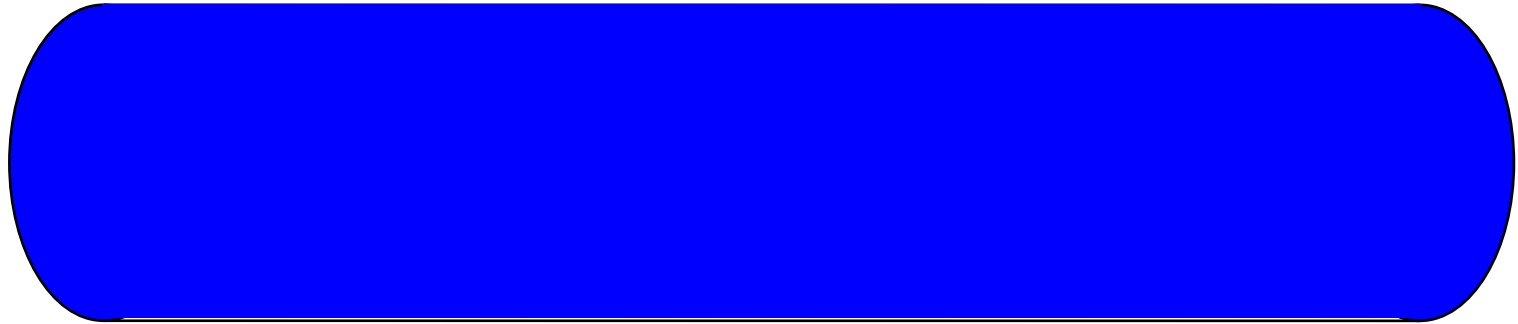
# Kind of like water in a pipe...

- To understand Z, let's make an analogy
  - Think of a wire as a pipe
    - Has water = 1
    - Has water = 0
  - This wire is 0 (it has no water)



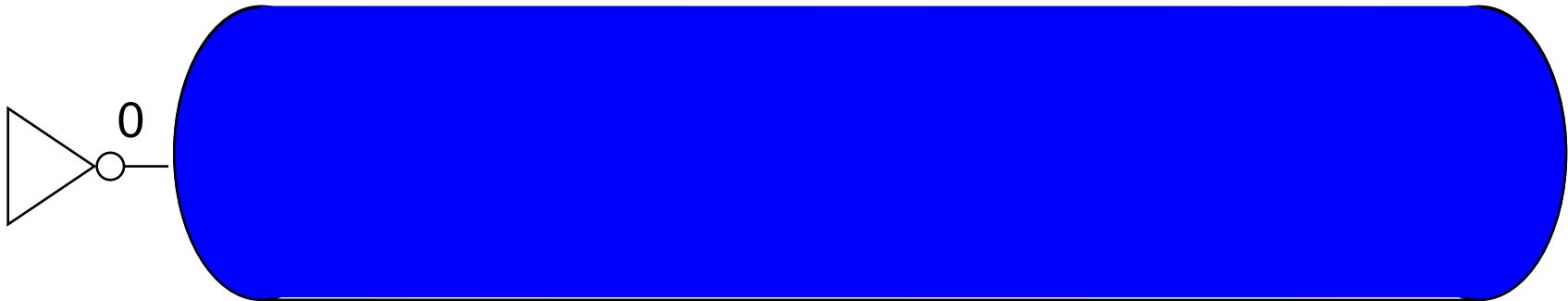
# Kind of like water in a pipe...

- To understand Z, let's make an analogy
  - Think of a wire as a pipe
    - Has water = 1
    - Has water = 0
  - This wire is 1 (it is full of water)



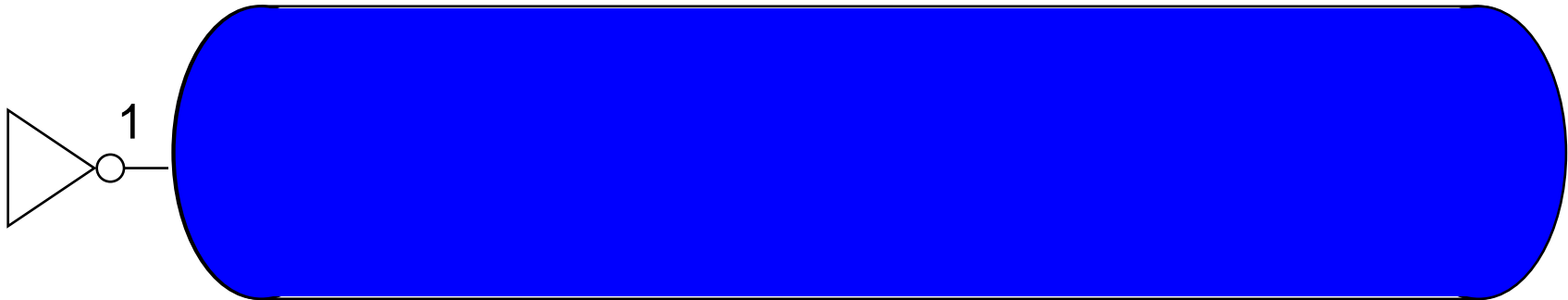
# Kind of like water in a pipe...

- To understand Z, let's make an analogy
  - Think of a wire as a pipe
    - Has water = 1
    - Has water = 0
  - Suppose a gate drives a 0 onto this wire
    - Think of it as sucking the water out



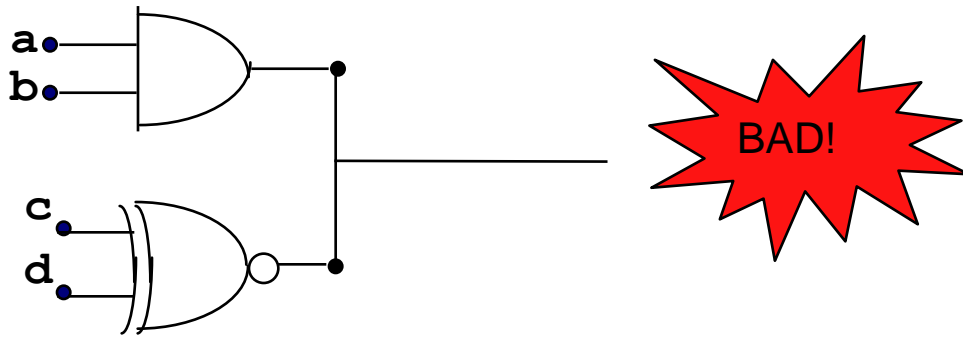
# Kind of like water in a pipe...

- To understand Z, let's make an analogy
  - Think of a wire as a pipe
    - Has water = 1
    - Has water = 0
  - Suppose the gate now drives a 1
    - Think of it as pumping water in



# Remember this rule?

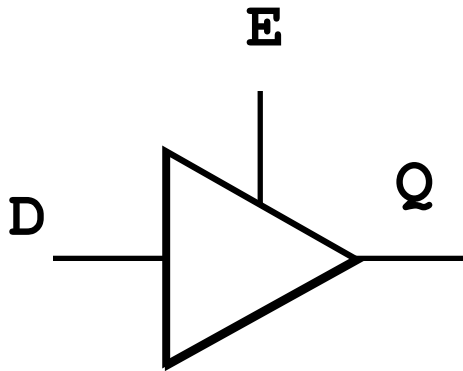
- Remember I told you not to connect two outputs?



- If one gate tries to drive a 1 and the other drives a 0
  - One pumps water in.. The other sucks it out
  - Except it's electric charge, not water
  - "Short circuit" → lots of current → lots of heat

## So this third option: Z

- There is a third possibility: Z (“high impedance”)
  - Neither pushing water in, nor sucking it out
  - Just closed off/blocked
  - Prevents electricity from flowing through
- Gate that gives us Z : **Tri-state**

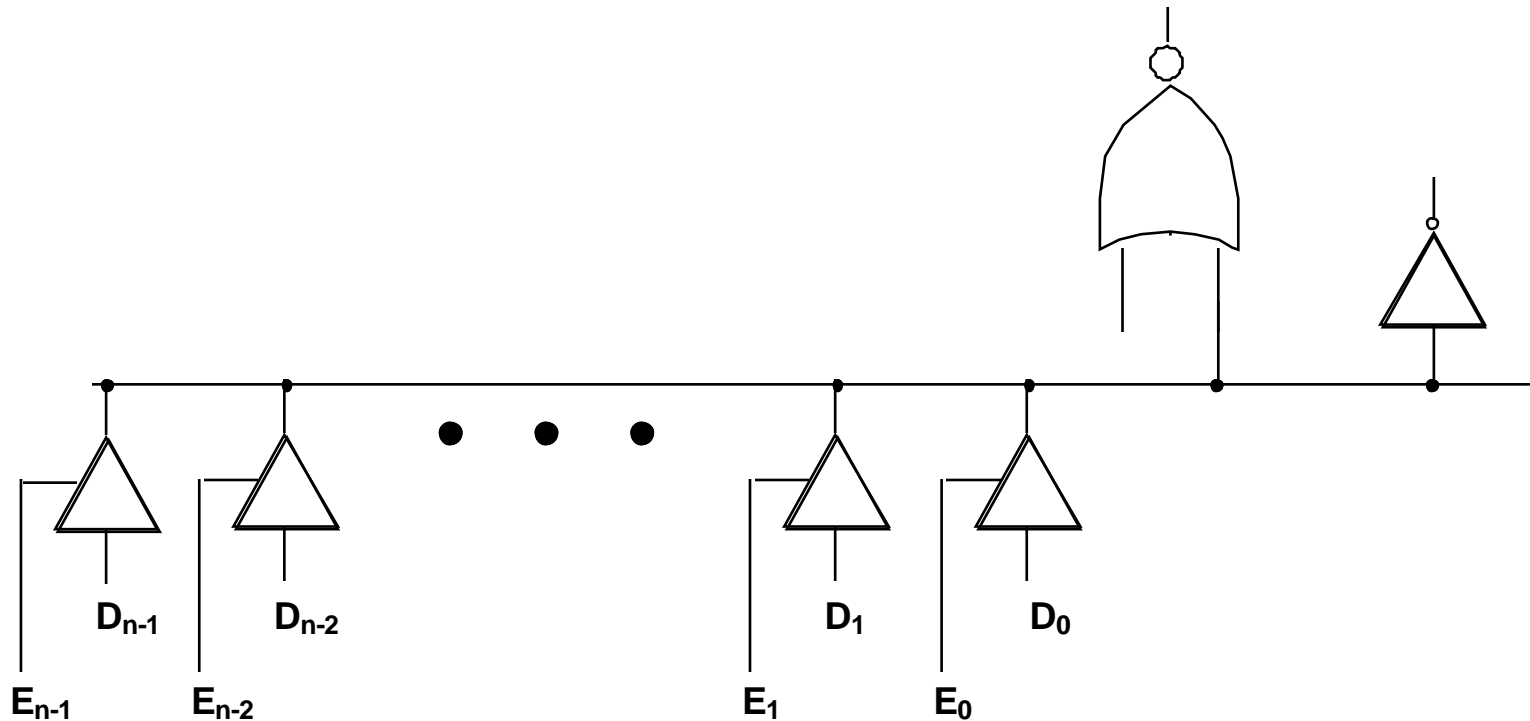


D	E	Q
0	1	0
1	1	1
-	0	Z

# We've had this rule one day... and you break it

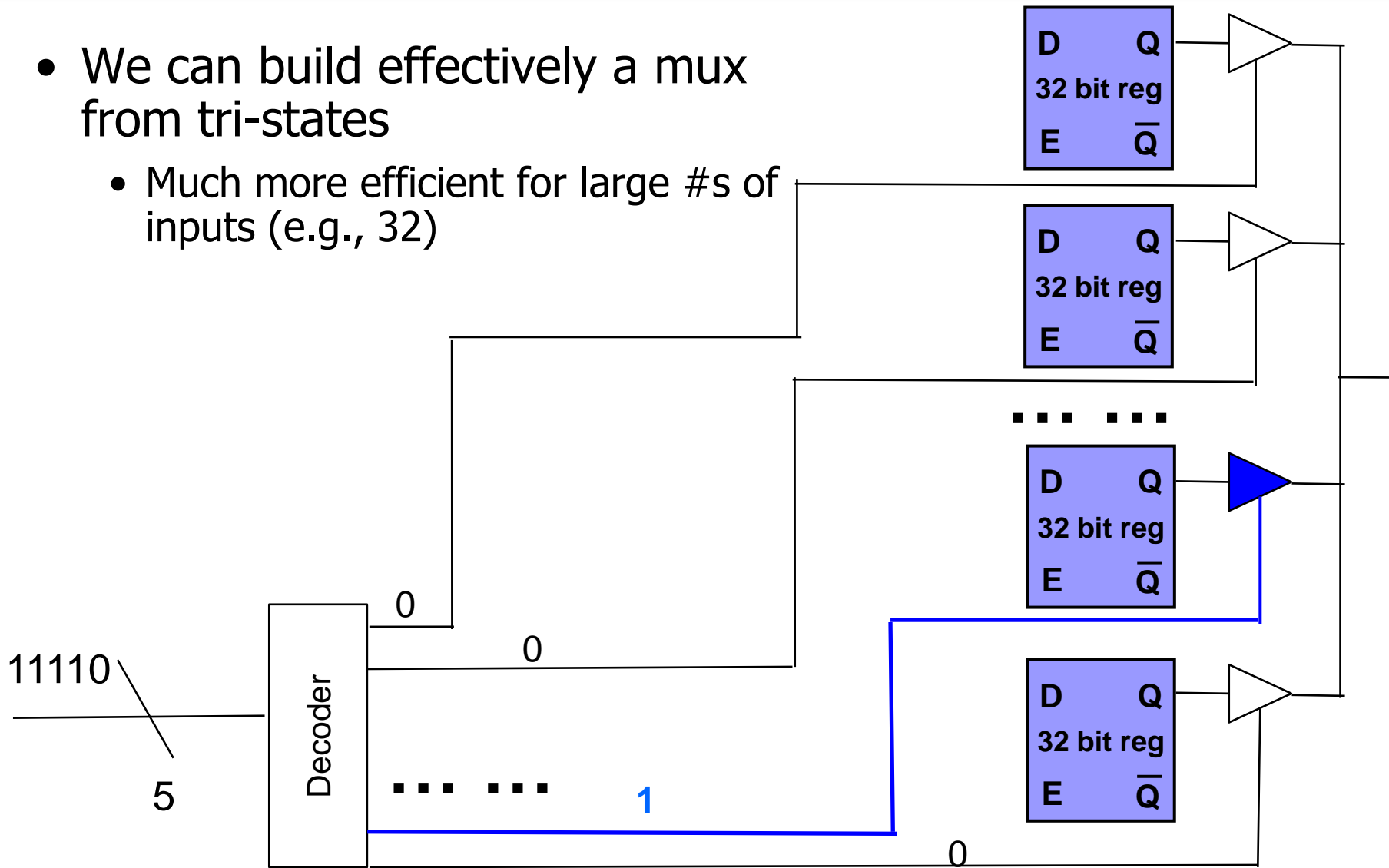
It's ok to connect multiple outputs together  
Under one circumstance:

**All but one** must be outputting Z at any time



# Mux, implemented with tri-states

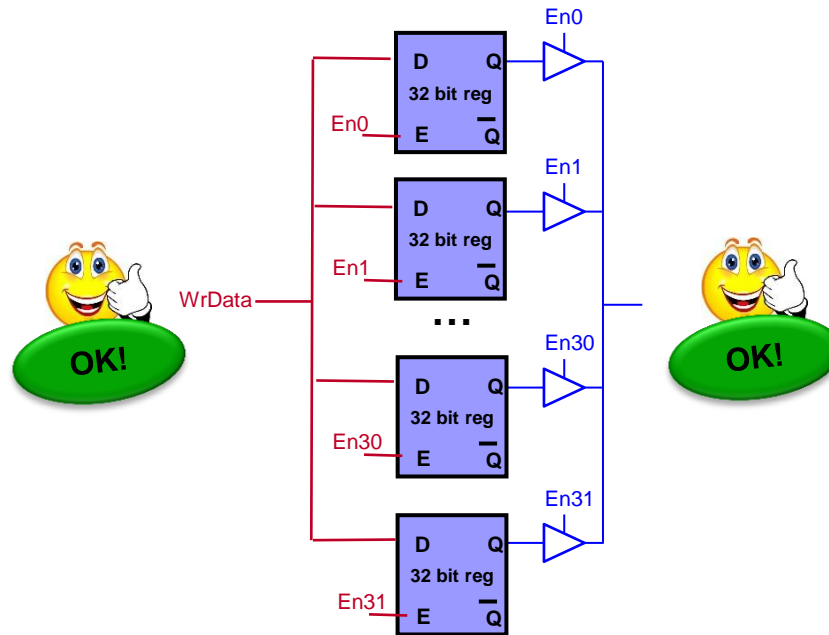
- We can build effectively a mux from tri-states
  - Much more efficient for large #s of inputs (e.g., 32)





# Register File

- Now we can **write** and **read** in one clock cycle!



# Ports

- What we just saw: **read** port
  - Ability to do one read / clock cycle
  - May want more: read 2 source registers per instr
    - Maybe even more if we do many instrs at once
  - This design: can just replicate port
    - Another decoder
    - Another set of tri-states
    - Another output bus (wire connecting the tri-states)
- Earlier: **write** port
  - Ability to do one write/cycle
  - Could add more: need muxes to pick wr values

# Minor Detail

- FYI: This is not how a modern register file is implemented
  - (Though it is how other things are implemented)
  - Actually done with SRAM
  - We'll see that later this semester...

# Summary

Can layout logic to compute things

Add, subtract,...

Now can store things

D flip-flops

Registers

Also understand clocks

Just about ready to make a datapath!