

PRACTICE MIDTERM EXAM FOR COMPSCI/ECE 250

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These questions are pasted in from various sources; ignore the question numbers and point values. Answers to SOME questions are provided in [blue](#).

Practice question 1

1) [10 points]

(a) Add the following base-10 numbers using **6-bit** 2s complement math: -3, -4. **Show your work!**

To get -3 in binary, start with 3 and negate (flip all bits and add one):

```
000011
111100 < bits flipped
111101 < added one
^ this is -3
```

Same to get -4 in binary:

```
000100
111011 < bits flipped
111100 < added one
^ this is -4 in binary
```

Now we add:

```
  1111 < carries
 111101
+ 111100
-----
111001 < sum
```

Check our work -- let's convert the sum to decimal. first we negate it to make it positive:

```
111001
000110 < bits flipped
000111 < added one
^ this is the negation of our sum
```

111 in binary is 7 in decimal

this makes sense, as $-3 + -4 = -7$

Practice question 2

2) Assume that \$2 = 2000 and \$3=12. Assume that memory holds the values at the addresses shown on the left. “lw” = load word, and “sw” = store word.

(a) If the computer executes sw \$3, 4(\$2), then what is the value of \$3 after this instruction?

12

(the store doesnt change the register, it changes the memory)

(b) If, after the instruction in part (a), the computer executes lw \$3, 0(\$2), what is the value of \$3 after this instruction?

130

(c) What single instruction could you use to write the value in \$5 into address 2008?

sw \$5, 8(\$2)

or as a joke answer: sw \$5, 1878(\$3)

(d) What single instruction could you use to read the word of memory at address 1996 and put the result in \$8?

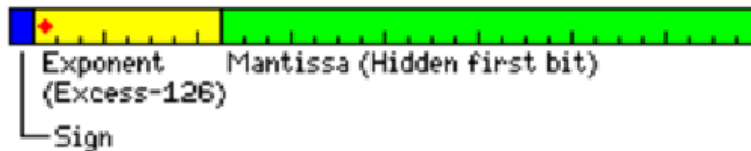
lw \$8, -4(\$2)

memory

address 2004	-52 12
address 2000	130

Practice question 3

3) [10] The IEEE 754 floating point standard specifies that 32-bit floating point numbers have one sign bit, an 8-bit exponent (with a bias of 127), and a 23-bit significand (with an implicit “1”). Represent the number -11.75 in this format.



Sign bit: 1 (negative)
Fractional representation: $-11 \frac{3}{4}$
Binary representation: -1011.11
Binary representation, normalized: $-1.01111 \cdot 2^3$
Mantissa with the first one removed: 01111
Exponent with bias added: $3+127 = 130$
Biased exponent in binary: 1000010

1 1000010 01111000000000000000000

Practice question 4

4) [10] The following questions are based on the following code snippet.

(a) What is `*(array+7)` ? Please give its datatype and its value.

Same as `array[7]`
Type: `int`
Value: 49

(b) On a MIPS machine, how big (how many bytes) is the variable `array`?

The variable `array`, like all pointers on a system with 32-bit words, is 32-bits long, which is 4 bytes long.

(c) On a MIPS machine, how big (how many bytes) is `array[2]`?

It's the size of an integer, which on MIPS, is 32-bits, or 4 bytes.

(c) What is the datatype of `fun`?

`int**`

(A pointer to a pointer to an int. Size is still 4 bytes, since it's a pointer)

```
int* array = (int*) malloc(42*sizeof(int));
int** fun = &array;
for (int i=0; i<42; i++){
    array[i] = i*i;
}
free (array);
```

Practice question 5

5) [25] Convert the following C code for the function foo() into MIPS code. **Use appropriate MIPS conventions for procedure calls**, including the passing of arguments and return values, as well as the saving/restoring of registers. Assume that there are 2 argument registers (\$a0-\$a1), 2 return value registers (\$v0-\$v1), 3 general-purpose callee-saved registers (\$s0-\$s2), and 3 general-purpose caller-saved registers (\$t0-\$t2). Assume \$ra is callee-saved. The C code is obviously somewhat silly and unoptimized, but YOU MAY NOT OPTIMIZE IT -- you must simply translate it as is.

```
1: int foo (int num){
2:   int temp = 0; //temp MUST be held in $t0
3:   if (num <0) {
4:       temp = num + 2;
5:   }else{
6:       temp = num - 2;
7:   }
8:   int sumA = bar(temp); // sumA MUST be held in $s0
9:   int sumB = sumA + temp + num; // sumB MUST be held in $s1
10:  return (sumB + 2);
11:}

12: int bar (int arg){
```

line(s) of C	instruction(s)	what code MUST do (if not obvious from C code)
1	<pre># need 20 bytes for s0,s1,t0,t1,ra # why t1 even though its not needed in the problem? # because i need to backup a0 before the call addiu \$sp,\$sp,-20 sw \$s0,0(\$sp) sw \$s1,4(\$sp) sw \$ra, 8(\$sp)</pre>	create stack frame large enough for callee-saved and caller-saved registers; save callee-saved registers (ONLY necessary ones)
2	<pre>li \$t0, \$t0, 0 # alternately, i could do "move \$t0,\$0"</pre>	
3-7	<pre>bgez \$a0, else # invert the compare to get to the else #then addi \$t0, \$a0, 2 j end_if # bypass the else else: addi \$t0, \$a0, -2 end_if:</pre>	
8	<pre>move \$t1,\$a0 # backup num move \$a0, \$t0 sw \$t0, 12(\$sp) sw \$t1, 16(\$sp) jal bar</pre>	save caller-saved registers (ONLY necessary ones); call bar() with appropriate arguments
after line 8	<pre>lw \$t0, 12(\$sp) lw \$t1, 16(\$sp) mov \$s0, \$v0</pre>	restore caller-saved registers; get value returned from bar() and put it in appropriate place
9	<pre>add \$s1, \$s0, \$t0 # sumA+temp add \$s1, \$s1, \$t1 # += num</pre>	
10	<pre>addi \$v0, \$s1, 2 lw \$s0,0(\$sp) lw \$s1,4(\$sp) lw \$ra, 8(\$sp) addiu \$sp, \$sp, 20 jr \$ra</pre>	pass return value back to whoever called foo(); restore callee-saved registers; destroy stack frame; return to caller

Practice question 6

1) [10 points] Write the truth table for the output of the following boolean expression that has three inputs (a, b, c): $output = abc + \bar{a}c + b\bar{c}$

a	b	c	output
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

Practice question 7

2) [10 points] Convert the following truth table into a boolean expression in product-of-sums format. Note that there are three inputs (a,b,c) and one output. Do NOT simplify or optimize in any way.

a	b	c	output
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

$(!a \& !b \& !c) \mid (!a \& b \& c) \mid (a \& !b \& c) \mid (a \& b \& !c) \mid (a \& b \& c)$

Practice question 8

Simplify this expression; axioms are provided ->

$$(!A \& B \& C) \mid (A \& B \& !C) \mid (A \& B \& C)$$

Factor (A&B)

$$(!A \& B \& C) \mid ((A \& B) \& (!C \mid C))$$

Inverse law

$$(!A \& B \& C) \mid ((A \& B) \& \text{true})$$

Identity law

$$(!A \& B \& C) \mid (A \& B)$$

Factor B

$$B \& (!A \& C) \mid A$$

Distribute A

$$B \& (!A \mid A) \& (C \mid A)$$

Inverse law

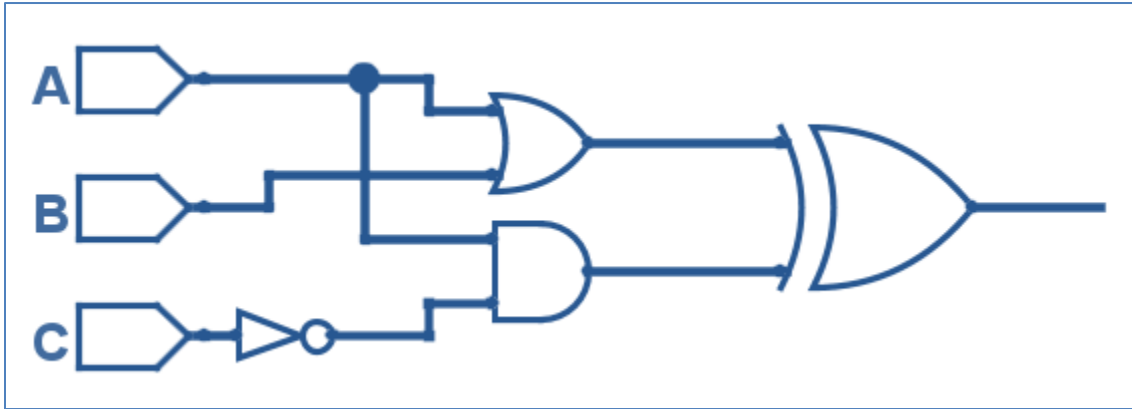
$$B \& (\text{true} \& (C \mid A))$$

Identity law

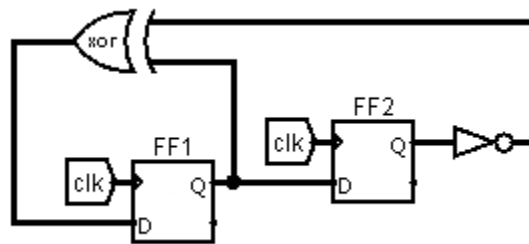
$$B \& (C \mid A)$$

Name	Definition
Identity law	$1 \& A = A$ $0 \mid A = A$
Null law	$0 \& A = 0$ $1 \mid A = 1$
Idempotent law	$A \& A = A$ $A \mid A = A$
Inverse law	$A \& !A = 0$ $A \mid !A = 1$
Commutative law	$A \& B = B \& A$ $A \mid B = B \mid A$
Associative law	$(A \& B) \& C = A \& (B \& C)$ $(A \mid B) \mid C = A \mid (B \mid C)$
Distributive law	$A \mid (B \& C) = (A \mid B) \& (A \mid C)$ $A \& (B \mid C) = (A \& B) \mid (A \& C)$
Absorption law	$A \& (A \mid B) = A$ $A \mid (A \& B) = A$
De Morgan's law	$!(A \& B) = !A \mid !B$ $!(A \mid B) = !A \& !B$
Double negation law	$!!A = A$

Practice question 9: Sketch a circuit representation of the expression $(A \mid B) \wedge (A \& !C)$



Practice question 10: Consider the circuit below. Assuming the two flip flop start with a value of zero, what will the state of the flip flops be for the clock cycles shown? The initial state is done for you.

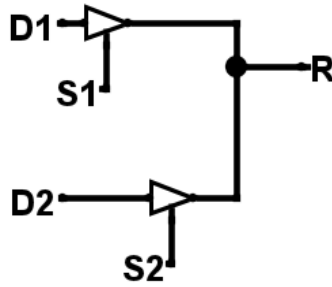


Clock cycle	FF1	FF2
0	0	0
1	1	0
2	0	1
3	0	0

Same exercise, but with a different starting condition:

Clock cycle	FF1	FF2
0	1	1
1	1	1
2	1	1

Practice question 11: The circuit below shows two tri-state buffers.



- (a) How could you make D1's value appear on output R?
Set S1 to 1 and S2 to 0.
- (b) How could you make D2's value appear on output R?
Set S1 to 0 and S2 to 1.
- (c) How could you make the output R be in the high-impedance ("Z") state?
Set both S1 and S2 to 0.
- (d) How could you cause a short circuit?
Set D1 to 1 and D2 to 0, then turn on both S1 and S2.

Practice question 12: Draw a finite state machine that will output a 1 if and only if a sequence of characters of the following form is received: exactly one 'D', zero or more 'O's, and exactly one 'G'. (If you happen to know regular expression notation, this is the expression /DO*G/.) Examples of matching inputs include: "DG", "DOG", "DOOOOG". Your machine can be of the Mealy or Moore variety. It doesn't matter what your machine does after it outputs 1.

