ECE/CS 250 Computer Architecture

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From C to Binary

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Also contains material adapted from CSC230: C and Software Tools developed by the NC State Computer Science Faculty

Outline

- Previously:
 - Computer is machine that does what we tell it to do
- Next:
 - How do we tell computers what to do?
 - How do we represent data objects in binary?
 - How do we represent data locations in binary?

Representing High Level Things in Binary

- Computers represent everything in binary
- Instructions are specified in binary
- Instructions must be able to describe
 - Operation types (add, subtract, shift, etc.)
 - Data objects (integers, decimals, characters, etc.)
 - Memory locations

• Example:

```
int x, y; // Where are x and y? How to represent an int? bool decision; // How do we represent a bool? Where is it? y = x + 7; // How do we specify "add"? How to represent 7? decision=(y>18); // Etc.
```

Representing Operation Types

- How do we tell computer to add? Shift? Read from memory?
 Etc.
- Arbitrarily!
- Each Instruction Set Architecture (ISA) has its own binary encodings for each operation type
- E.g., in MIPS:
 - Integer add is: 00000 010000
 - Read from memory (load) is: 010011
 - Etc.

Representing Data Types

- How do we specify an integer? A character? A floating point number? A bool? Etc.
- Same as before: binary!

Data and interpretation are separate:

 The same 32 bits might mean one thing if interpreted as an integer, but another thing if interpreted as a floating point number

Basic Data Types

Bit String: sequence of bits of a particular length
4 bits is a nibble
8 bits is a byte
16 bits is a half-word (for MIPS32)

16 bits is a half-word (for MIPS32)
32 bits is a word (for MIPS32)

64 bits is a double-word (for MIPS32)

128 bits is a quad-word (for MIPS32)

What is a <u>word</u>?
The standard unit of manipulation

for a particular system. E.g.:

- MIPS32: 32 bits
- Original Nintendo: 8 bit
- Super Nintendo: 16 bit
- Intel x86 (classic): 32 bit
- Nintendo 64: 64 bit
- Intel x86 64 (modern): 64 bit

Integers (char, short, int, long):

"2's Complement" (32-bit or 64-bit representation)

Floating Point (float, double):

Single Precision (32-bit representation)

Double Precision (64-bit representation)

Extended (Quad) Precision (128-bit representation)

<u>Character (char):</u>

Bit (bool): 0, 1

char ASCII 7-bit code

Basic Binary

Advice: memorize the following

•
$$2^0 = 1$$

•
$$2^1 = 2$$

•
$$2^2 = 4$$

•
$$2^3 = 8$$

•
$$2^4 = 16$$

•
$$2^5 = 32$$

•
$$2^6 = 64$$

•
$$2^7 = 128$$

•
$$2^8 = 256$$

•
$$2^9 = 512$$

•
$$2^{10} = 1024$$



Bits vs things

If you have N bits, you can represent 2^N things.





If you have T things, you need log₂T bits to pick one.

You will have to answer questions of this form roughly a thousand times in this course — note it now!

- Exercises:
 - I have 8 bits, how many integers can I represent?
 - $2^8 = 256$
 - I need to represent 32 cache sets. How many bits do I need?
 - $\log_2 32 = 5$
 - I have 4GB of RAM. How many bits do I need to pick one byte of it?
 - log₂ 4G =?

Binary metric system

The binary metric system:

- $2^{10} = 1024$.
- This is *basically* 1000, so we can have an alternative form of metric units based on base 2.
- 2^{10} bytes = 1024 bytes = 1kB.
 - Sometimes written as 1kiB
 (pronounced "ki<u>bi</u>byte" where the 'bi' means 'binary')
 (but nobody says "kibibyte" out loud because it sounds stupid)
- 2^{20} bytes = 1MB, 2^{30} bytes = 1GB, 2^{40} bytes = 1TB, etc.
- Easy rule to convert between exponent and binary metric number:

$$2^{XY}$$
 bytes = $2^{Y} \cdot 2^{X0}$ bytes = $2^{Y} < X_prefix>B$



$$2^{13}$$
 bytes = 2^{3} kB = 8 kB 2^{39} bytes = 2^{9} GB = 512 GB

$$2^{05}$$
 bytes = 2^{5} B = 32 B

From last slide: $log_2 4G = 32$

What does it mean to say base 10 or base 2?

• Integers in regular base 10:

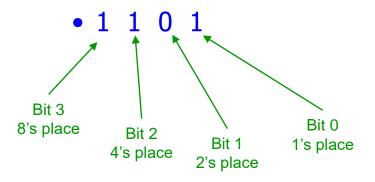
• 6253 =
$$6000 + 200 + 50 + 3$$

= $6*10^3 + 2*10^2 + 5*10^1 + 3*10^0$
Digit Base Place

Integers in base 2:

• 1101 =
$$1000 + 100 + 00 + 1$$

= $1*2^3 + 1*2^2 + 0*2^1 + 1*2^0$
= $8 + 4 + 1$
= 13



Decimal to binary using remainders

?	Quotient	Remainder	
457 ÷ 2 =	228	1	
228 ÷ 2 =	114	0 —	
114 ÷ 2 =	57	0 —	
57 ÷ 2 =	28	1	
28 ÷ 2 =	14	0 —	
14 ÷ 2 =	7	0 —	
7 ÷ 2 =	3	1	
3 ÷ 2 =	1	1	
1 ÷ 2 =	0	1	→111001001

Decimal to binary using comparison

			111001001
Num	Compare 2 ⁿ	≥?	
457	256	1 ~	
201	128	1	
73	64	1	
9	32	0	
9	16	0	
9	8	1 ~	
1	4	0 ~	
1	2	0 ~	
1	1	1	

Hexadecimal

Indicates a hex number

Hex digit	Binary	Decimal
0	0000	0
1	0001	1
2	0010	2
3	0011	3
4	0100	4
5	0101	5
6	0110	6
7	0111	7
8	1000	8
9	1001	9
A	1010	10
В	1011	11
С	1100	12
D	1101	13
E	1110	14
F	1111	15

OXDEADBEEF

1101 1110 1010 1101 1011 1110 1110 1111

0x02468ACE

0x13579BDF

0001 0011 0101 0111 1001 1011 1101 1111



Binary to/from hexadecimal

- 0101101100100011₂ -->
- 0101 1011 0010 0011₂ -->
- 5 B 2 3₁₆

0001 1111 0100 1011₂ -->

00011111010010112

Hex digit	Binary	Decimal	
0	0000	0	
1	0001	1	
2	0010	2	
3	0011	3	
4	0100	4	
5	0101	5	
6	0110	6	
7	0111	7	
8	1000	8	
9	1001	9	
A	1010	10	
В	1011	11	
С	1100	12	
D	1101	13	
E	1110	14	
F	1111	15	

BitOps: Unary

- Bit-wise complement (~)
 - Flips every bit.

```
~0x0d // (binary 00001101)
== 0xf2 // (binary 11110010)
```

Not the same as Logical NOT (!) or sign change (-)

BitOps: Two Operands

- Operate bit-by-bit on operands to produce a result operand of the same length
- And (&): result 1 if both inputs 1, 0 otherwise
- Or (|): result 1 if either input 1, 0 otherwise
- Xor (^): result 1 if one input 1, but not both, 0 otherwise
- Useful identities (applied per-bit):

```
• X & 1 = X ANDing with 1 does nothing
```

•
$$x & 0 = 0$$
 ANDing with 0 gives zero

•
$$X \mid 0 = X$$
 ORing with 0 does nothing

•
$$X \mid 1 = 1$$
 ORing with 1 gives one

•
$$x ^0 = x$$
 XORing with 0 does nothing

•
$$x ^1 = x$$
 XORing with 1 flips the bit

Two Operands... (cont'd)

Examples

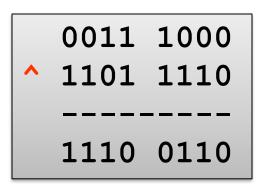
```
0011 1000

1101 1110

-----

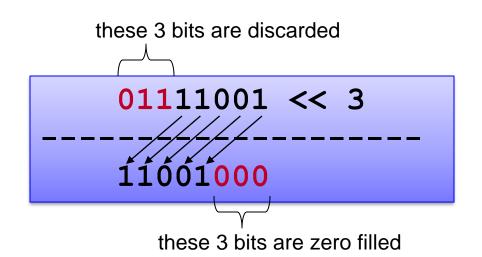
0001 1000
```

```
0011 1000
| 1101 1110
| -----
| 1111 1110
```



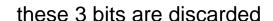
Shift Operations

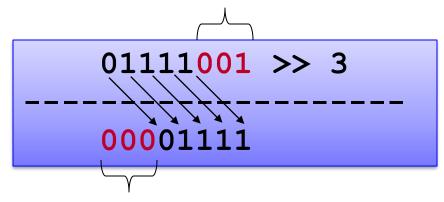
- x << y is left (logical) shift of x by y positions
 - x and y must both be integers
 - x should be unsigned or positive
 - y leftmost bits of x are discarded
 - zero fill y bits on the right



ShiftOps... (cont'd)

- x >> y is right (logical) shift of x by y positions
 - y rightmost bits of x are discarded
 - zero fill y bits on the left





these 3 bits are zero filled

Bitwise Recipes

- Set a certain bit to 1?
 - Make a MASK with a *one* at every position you want to *set*:

```
m = 0x02; // 0000010_2
```

• OR the mask with the input:

```
v = 0x41; // 01000001_2

v = m; // 0100001_2
```

- Clear a certain bit to 0?
 - Make a MASK with a zero at every position you want to clear.

```
m = 0xFD; // 111111101<sub>2</sub> (could also write ~0x02)
```

AND the mask with the input:

```
v = 0x27; // 00100111<sub>2</sub>

v \&= m; // 00100101<sub>2</sub>
```

- Get a substring of bits (such as bits 2 through 5)? *Note: bits are numbered right-to-left starting with zero.*
 - Shift the bits you want all the way to the right then AND them with an appropriate mask:

```
v = 0x67; // 01100111_2

v >>= 2; // 00011001_2

v &= 0x0F; // 00001001_2
```

Suppose we want to add two numbers:

```
00011101
+ 00101011
```

How do we do this?

$$00011101$$
 695
+ 00101011 + 232

- How do we do this?
 - Let's revisit decimal addition
 - Think about the process as we do it

Suppose we want to add two numbers:

$$\begin{array}{c} 00011101 & 695 \\ + 00101011 & + 232 \\ \hline 7 \end{array}$$

• First add one's digit 5+2 = 7

- First add one's digit 5+2 = 7
- Next add ten's digit 9+3 = 12 (2 carry a 1)

$$\begin{array}{c} 00011101 & 695 \\ + 00101011 & + 232 \\ \hline 927 \end{array}$$

- First add one's digit 5+2 = 7
- Next add ten's digit 9+3 = 12 (2 carry a 1)
- Last add hundred's digit 1+6+2 = 9

```
00011101 + 00101011
```

- Back to the binary:
- First add 1's digit 1+1 = ...?

```
1
00011101
+ 00101011
0
```

- Back to the binary:
- First add 1's digit 1+1 = 2 (0 carry a 1)

```
11
00011101
+ 00101011
00
```

- Back to the binary:
- First add 1's digit 1+1 = 2 (0 carry a 1)
- Then 2's digit: 1+0+1=2 (0 carry a 1)
- You all finish it out....

Suppose we want to add two numbers:

```
\begin{array}{rcl}
111111 \\
00011101 &= 29 \\
+ & 00101011 &= 43 \\
\hline
01001000 &= 72
\end{array}
```

Can check our work in decimal

Issues for Binary Representation of Numbers

How to represent negative numbers?

- There are many ways to represent numbers in binary
 - Binary representations are encodings → many encodings possible
 - What are the issues that we must address?
- Issue #1: Complexity of arithmetic operations
- Issue #2: Negative numbers
- Issue #3: Maximum representable number
- Choose representation that makes these issues easy for machine, even if it's not easy for humans (i.e., ECE/CS 250 students)
 - Why? Machine has to do all the work!

Sign Magnitude

- Use leftmost bit for +(0) or -(1):
- 6-bit example (1 sign bit + 5 magnitude bits):
- \bullet +17 = 010001
- \bullet -17 = 110001
- Pros:
 - Conceptually simple
 - Easy to convert
- Cons:
 - Harder to compute (add, subtract, etc) with
 - Positive and negative 0: 000000 and 100000



1's Complement Representation for Integers

- Use largest positive binary numbers to represent negative numbers
- To negate a number,

```
invert ("not") each bit: 0 \rightarrow 1
```

$$1 \rightarrow 0$$

- Cons:
 - Still two 0s (yuck)
 - Still hard to compute with

0000	0
0001	1
0010	2
0011	3
0100	4
0101	5
0110	6
0111	7
1000	-7
1001	-6
1010	-5
1011	-4
1100	-3
1101	-2
1110	-1
1111	-0



2's Complement Integers

- Use large positives to represent negatives
- $(-x) = 2^n x$
- This is 1's complement + 1
- $(-x) = 2^n 1 x + 1$
- So, just invert bits and add 1

6-bit examples:

$$010110_2 = 22_{10}$$
; $101010_2 = -22_{10}$
 $1_{10} = 000001_2$; $-1_{10} = 1111111_2$
 $0_{10} = 0000000_2$; $-0_{10} = 0000000_2 \rightarrow \text{good}$

	1010	-6
$= -22_{10}$	1011	-5
.111 ₂	1100	-4
<u>-</u>	1101	-3
$1000_2 \rightarrow \text{good!}$	1110	-2
	1111	-1
7115		



Another way to think about 2's complement

• Regular base 10:

• 6253 =
$$6000 + 200 + 50 + 3$$

= $6*10^3 + 2*10^2 + 5*10^1 + 3*10^0$
Digit Base Place

Unsigned base 2:

• 1101 =
$$1000 + 100 + 00 + 1$$

= $1*2^3 + 1*2^2 + 0*2^1 + 1*2^0$
= $8 + 4 + 1$
= 13

Signed base 2:

• 1101 = -1000 + 100 + 00 + 1
=
$$1*-2^3 + 1*2^2 + 0*2^1 + 1*2^0$$

= $-8 + 4 + 1$
= -3

Alternately, flip the bits and add 1:

1101

Flip: 0010 +1: 0011

That's 3 in binary, so the number is indeed -3

Two's complement is like making the highest order bit apply a negative value!

Pros and Cons of 2's Complement

Advantages:

- Only one representation for 0 (unlike 1's comp): 0 = 000000
- Addition algorithm is much easier than with sign and magnitude
 - Independent of sign bits

Disadvantage:

- One more negative number than positive
- Example: 6-bit 2's complement number $100000_2 = -32_{10}$; but 32_{10} could not be represented

All modern computers use 2's complement for integers

Integer ranges

Remember: if you have N bits, you can represent 2^N things

- If I have an n-bit integer:
 - And it's **unsigned**, then I can represent $\{0 \dots 2^n 1\}$
 - And it's **signed**, then I can represent $\{-(2^{n-1}) \dots 2^{n-1} 1\}$



• Result:

Size in bits	Size in bytes	Datatype	Unsigned range	Signed range
8	1	char	0 255	-128 127
16	2	short	0 65,535	-32,768 32,767
32	4	int	0 4,294,967,295	-2,147,483,648 2,147,483,647
64	8	long long	0 18,446,744,073,709,600,000	-9,223,372,036,854,780,000 9,223,372,036,854,780,000

```
How to get unsigned integers in C? Just say unsigned:

int x; // defaults to signed
unsigned int y; // explicitly unsigned
```

2's Complement Precision Extension

- Most computers today support 32-bit (int) or 64-bit integers
 - Specify 64-bit using gcc C compiler with long long
- To extend precision, use sign bit extension
 - Integer precision is number of bits used to represent a number

Examples

```
14_{10} = 001110_2 in 6-bit representation.
```

 $14_{10} = 000000001110_2$ in 12-bit representation

```
-14_{10} = 110010_2 in 6-bit representation
```

 $-14_{10} = 11111111110010_2$ in 12-bit representation.

Binary Math: Addition

• Let's look at another binary addition:

```
01011101
+ 01101011
```

Binary Math: Addition

What about this one:

```
\begin{array}{rcl}
11111111 \\
01011101 &= 93 \\
+ & 01101011 &= 107 \\
\hline
11001000 &= -56
\end{array}
```

- But... that can't be right?
 - What do you expect for the answer?
 - What is it in 8-bit signed 2's complement?

Integer Overflow

- Answer should be 200
 - Not representable in 8-bit signed representation
 - No right answer
- This is called integer Overflow
- Real problem in programs
- How to solve?



Subtraction

- 2's complement makes subtraction easy:
 - Remember: A B = A + (-B)
 - And: $-B = \sim B + 1$
 - ↑ that means flip bits ("not")
 - So we just flip the bits and start with carry-in (CI) = 1
 - Later: No new circuits to subtract (re-use adder hardware!)

What About Non-integer Numbers?

- There are infinitely many real numbers between two integers
- Many important numbers are real
 - Speed of light $\sim = 3x10^8$
 - Pi = 3.1415...
- Fixed number of bits limits range of integers
 - Can't represent some important numbers
- Humans use Scientific Notation
 - 1.3x10⁴

Option 1: Fixed point

- Use normal integers, but (X*2^K) instead of X
 - Example: 32 bit int, but use X*65536
 - 3.1415926 * 65536 = 205887
 - 0.5 * 65536 = 32768 , etc..
- Pros:
 - Addition/subtraction just like integers ("free")
- Cons:
 - Mul/div require renormalizing (divide by 64K)
 - Range limited (no good rep for large + small)
- Can be good in specific situations

Can we do better?

- Think about scientific notation for a second:
- For example:

```
6.02 * 10^{23}
```

- Real number, but comprised of ints:
 - 6 generally only 1 digit here
 - 02 any number here
 - 10 always 10 (base we work in)
 - 23 can be positive or negative
- Can we do something like this in binary?

Option 2: Floating Point

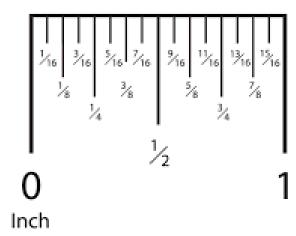
- How about:
 +/- X.YYYYYY * 2+/-N
- Big numbers: large positive N
- Small numbers (<1): negative N
- Numbers near 0: small N
- This is "floating point": most common way

IEEE single precision floating point

- Specific format called IEEE single precision:
 +/- 1.YYYYY * 2^(N-127)
- "float" in Java, C, C++,...
- Assume first bit is always 1 (saves us a bit)
- 1 sign bit (+ = 0, 1 = -)
- 8 bit biased exponent (do N-127)
- Implicit 1 before binary point
- 23-bit *mantissa* (YYYYY)

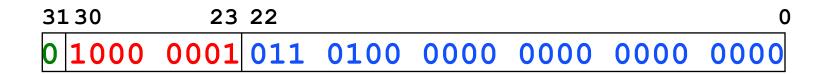
Binary fractions

- 1.YYYY has a binary point
 - Like a decimal point but in binary
 - After a decimal point, you have
 - tenths
 - hundredths
 - thousandths
 - ...
- So after a binary point you have...
 - Halves
 - Quarters
 - Eighths
 - ...



Floating point example

- Binary fraction example: $101.101 = 4 + 1 + \frac{1}{2} + \frac{1}{8} = 5.625$
- For floating point, needs normalization:
 1.01101 * 2²
- Sign is +, which = 0
- Exponent = $127 + 2 = 129 = 1000 \ 0001$
- Mantissa = 1.011 0100 0000 0000 0000 0000



Can use hex to represent those bits in a less annoying way:

Floating Point Representation

Example:

What floating-point number is:

0xC1580000?

Answer

What floating-point number is 0xC1580000?

1100 0001 0101 1000 0000 0000 0000 0000

Sign = 1 which is negative

Exponent =
$$(128+2)-127 = 3$$

Mantissa = 1.1011

$$-1.1011x2^3 = -1101.1 = -13.5$$

Trick question

- How do you represent 0.0?
 - Why is this a trick question?
 - \bullet 0.0 = 0.00000
 - But need 1.XXXXX representation?
- Exponent of 0 is denormalized
 - Implicit 0. instead of 1. in mantissa
 - Allows 0000....0000 to be 0
 - Helps with very small numbers near 0
- Results in +/- 0 in FP (but they are "equal")

Other Weird FP numbers

- Exponent = 1111 1111 also not standard
 - All 0 mantissa: $+/-\infty$ $1/0 = +\infty$

$$-1/0 = -\infty$$

Non zero mantissa: Not a Number (NaN)

$$sqrt(-42) = NaN$$

Floating Point Representation

Double Precision Floating point:

64-bit representation:

- 1-bit sign
- 11-bit (biased) exponent
- 52-bit fraction (with implicit 1).
- "double" in Java, C, C++, ...

S	Exp	Mantissa
1	11-bit	52 - bit

What About Strings?

- Many important things stored as strings...
 - E.g., your name
- How should we store strings?

Standardized ASCII (0-127)

Dec Hx Oct Char	Dec Hx Oct Html Chr	Dec Hx Oct Html Chr Dec Hx Oct Html Chr
0 0 000 NUL (null)	32 20 040 Spac	e 64 40 100 @ 0 96 60 140 ` `
l 1 001 SOH (start of heading)	33 21 041 6#33; !	65 41 101 6#65; A 97 61 141 6#97; a
2 2 002 STX (start of text)	34 22 042 @#34; "	66 42 102 a#66; B 98 62 142 a#98; b
3 3 003 ETX (end of text)	35 23 043 # #	67 43 103 a#67; C 99 63 143 a#99; C
4 4 004 EOT (end of transmission)	36 24 044 \$ 年	68 44 104 D D 100 64 144 d d
5 5 005 ENQ (enquiry)	37 25 045 % %	69 45 105 6#69; E 101 65 145 6#101; e
6 6 006 <mark>ACK</mark> (acknowledge)	38 26 046 & &	70 46 106 «#70; F 102 66 146 «#102; f
7 7 007 BEL (bell)	39 27 047 @#39; '	71 47 107 6#71; G 103 67 147 6#103; g
8 8 010 <mark>BS</mark> (backspace)	40 28 050 4#40; (72 48 110 6#72; H 104 68 150 6#104; h
9 9 011 TAB (horizontal tab)	41 29 051 6#41;)	73 49 111 6#73; I 105 69 151 6#105; i
10 A 012 LF (NL line feed, new line)		74 4A 112 6#74; J 106 6A 152 6#106; j
ll B 013 <mark>VT</mark> (vertical tab)	43 2B 053 + +	75 4B 113 6#75; K 107 6B 153 6#107; k
12 C 014 FF (NP form feed, new page)		76 4C 114 a#76; L 108 6C 154 a#108; L
13 D 015 CR (carriage return)	45 2D 055 - -	77 4D 115 6#77; M 109 6D 155 6#109; M
14 E 016 <mark>SO</mark> (shift out)	46 2E 056 . .	78 4E 116 N N 110 6E 156 n n
15 F 017 SI (shift in)	47 2F 057 / /	79 4F 117 6#79; 0 111 6F 157 6#111; 0
16 10 020 DLE (data link escape)	48 30 060 0 0	80 50 120 6#80; P 112 70 160 6#112; P
17 11 021 DC1 (device control 1)	49 31 061 @#49; 1	81 51 121 6#81; Q 113 71 161 6#113; q
18 12 022 DC2 (device control 2)	50 32 062 2 2	82 52 122 6#82; R 114 72 162 6#114; r
19 13 023 DC3 (device control 3)	51 33 063 3 3	83 53 123 6#83; S 115 73 163 6#115; S
20 14 024 DC4 (device control 4)	52 34 064 4 4	84 54 124 T T 116 74 164 t t
21 15 025 NAK (negative acknowledge)	53 35 065 4#53; 5	85 55 125 6#85; U 117 75 165 6#117; u
22 16 026 SYN (synchronous idle)	54 36 066 6 6	86 56 126 V V 118 76 166 v V
23 17 027 ETB (end of trans. block)	55 37 067 7 7	87 57 127 6#87; ₩ 119 77 167 6#119; ₩
24 18 030 CAN (cancel)	56 38 070 8 8	88 58 130 X X 120 78 170 x X
25 19 031 EM (end of medium)	57 39 071 9 9	89 59 131 6#89; Y 121 79 171 6#121; Y
26 lA 032 <mark>SUB</mark> (substitute)	58 3A 072 ::	90 5A 132 6#90; Z 122 7A 172 6#122; Z
27 1B 033 ESC (escape)	59 3B 073 ;;	91 5B 133 6#91; [123 7B 173 6#123; {
28 1C 034 FS (file separator)	60 3C 074 < <	92 5C 134 6#92; \ 124 7C 174 6#124;
29 1D 035 <mark>GS</mark> (group separator)	61 3D 075 = =	93 5D 135 6#93;] 125 7D 175 6#125; }
30 1E 036 RS (record separator)	62 3E 076 > >	94 5E 136 ^ ^ 126 7E 176 ~ ~
31 1F 037 <mark>US</mark> (unit separator)	63 3F 077 ? ?	95 5F 137 _ _ 127 7F 177 DEL

Source: www.LookupTables.com

One Interpretation of 128-255

128	Ç	144	É	161	í	177	******	193	Т	209	₹	225	ß	241	±
129	ü	145	88	162	ó	178		194	т	210	π	226	Γ	242	≥
130	é	146	Æ	163	ú	179		195	H	211	Ш	227	π	243	≤
131	â	147	ô	164	ñ	180	4	196	_	212	F	228	Σ	244	ſ
132	ä	148	ö	165	Ñ	181	4	197	+	213	F	229	σ	245	J
133	à	149	ò	166	2	182	-	198	% ⊨	214	IT.	230	μ	246	÷
134	å	150	û	167	۰	183	П	199	ŀ	215	#	231	τ	247	8
135	ç	151	ù	168	ė.	184	₹	200	L	216	+	232	Φ	248	۰
136	ê	152	_	169	١_١	185	4	201	F	217	J	233	Θ	249	
137	ë	153	Ö	170	-	186		202	<u>JL</u>	218	Г	234	Ω	250	
138	è	154	Ü	171	1/2	187	a	203	īΓ	219		235	8	251	\mathcal{A}
139	ï	156	£	172	3/4	188	1	204	l	220		236	00	252	_
140	î	157	¥	173	i	189	Ш	205	=	221		237	ф	253	2
141	ì	158	7	174	«	190	4	206	#	222		238	ε	254	
142	Ä	159	f	175	»	191	٦	207	<u></u>	223		239	\wedge	255	
143	Å	160	á	176		192	L	208	Ш	224	α	240	=		

Source: www.LookupTables.com

(This allowed totally sweet ASCII art in the 90s)



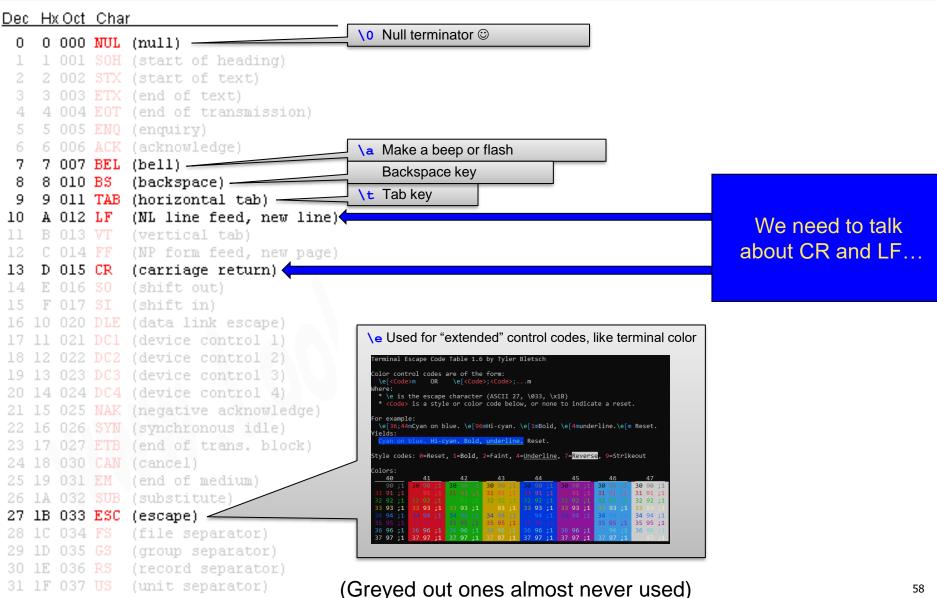


Sources:

- http://roy-sac.deviantart.com/art/Cardinal-NFO-File-ASCII-35664604
- http://roy-sac.deviantart.com/art/Siege-ISO-nfo-ASCII-Logo-35940815
- http://roy-sac.deviantart.com/art/deviantART-ANSI-Logo-31556803



About those control codes...



About CR and LF

History: first computer "displays" were modified typewriters



- $CR = "Carriage return" = \r = 0x0D$
 - Move typey part to the left → move cursor to left of screen
- LF = "Line feed" = $\n = 0x0A$
 - Move paper one line down → Move cursor one down
- Windows: "Pretend to be a typewriter"
 - Every time you press enter you get CR+LF (bytes 0D,0A)
- Linux/Mac: "You are not a typewriter"
 - Every time you press enter you get LF (byte 0A)
- This effects ALL TEXT DOCUMENTS!!!
 - Not all apps cope automatically! It will bite you one day for sure!

Outline

- Previously:
 - Computer is machine that does what we tell it to do
- Next:
 - How do we tell computers what to do?
 - How do we represent data objects in binary?
 - How do we represent data locations in binary?

Computer Memory

- Where do we put these numbers?
 - Registers [more on these later]
 - In the processor core
 - Compute directly on them
 - Few of them (~16 or 32 registers, each 32-bit or 64-bit)
 - Memory [Our focus now]
 - External to processor core
 - Load/store values to/from registers
 - Very large (multiple GB)

Memory Organization

- Memory: billions of locations...how to get the right one?
 - Each memory location has an address
 - Processor asks to read or write specific address
 - Memory, please load address 0x123400
 - Memory, please write 0xFE into address 0x8765000
 - Kind of like a giant array
 - Array of what?
 - Bytes?
 - 32-bit ints?
 - 64-bit ints?

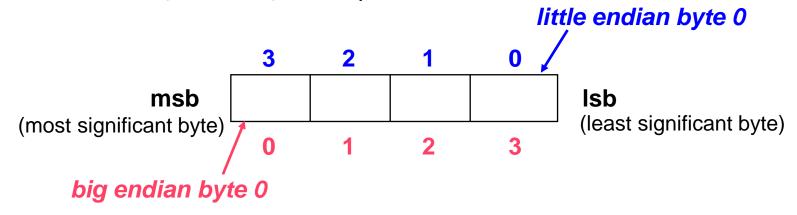
Memory Organization

- Most systems: byte (8-bit) addressed
 - Memory is "array of bytes"
 - Each address specifies 1 byte
 - Support to load/store 8, 16, 32, 64 bit quantities
 - Byte ordering varies from system to system
- Some systems "word addressed"
 - Memory is "array of words"
 - Smaller operations "faked" in processor
 - Not very common

Word of the Day: Endianess

Byte Order

- Big Endian: byte 0 is eight most significant bits MIPS, IBM 360/370, Motorola 68k, Sparc, HP PA
- Little Endian: byte 0 is eight least significant bits Intel 80x86, DEC Vax, DEC Alpha



Program

```
X = 0x12345678; // X lives at address 0x1000
```

0x1000:0x1001: 34 0x1002:56

0x1003:

Memory layout on a big endian system

Memory layout on a little endian system

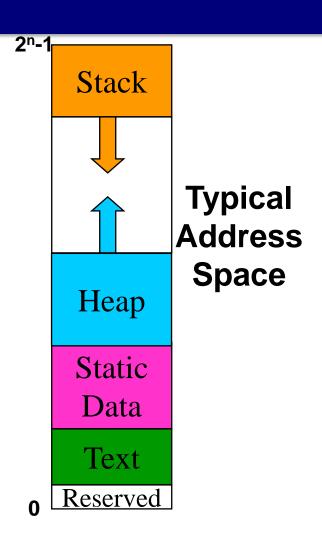
0x1000:0x1001: 56 0x1002: 34

78

 $0 \times 1003: 12$

Memory Layout

- Memory is array of bytes, but there are conventions as to what goes where in this array
- Text: instructions (the program to execute)
- Data: global variables
- Stack: local variables and other per-function state; starts at top & grows down
- Heap: dynamically allocated variables; grows up
- What if stack and heap overlap????



Memory Layout: Example

```
int anumber = 3;
int factorial (int x) {
                                                  Stack
  if (x == 0) {
    return 1;
                                                          Typical
  else {
                                                         Address
    return x * factorial (x - 1);
                                                          Space
                                                  Heap
                                                  Static
int main (void) {
                                                  Data
  int z = factorial (anumber);
                                                  Text
  int* p = malloc(sizeof(int)*64);
 printf("%d\n", z);
                                                Reserved
  return 0;
                      // p is a local on stack, *p is in heap
```

Summary: From C to Binary

- Everything must be represented in binary!
- Pointer is memory location that contains address of another memory location
- Computer memory is linear array of bytes
 - Integers:
 - unsigned {0..2ⁿ-1} vs signed {-2ⁿ⁻¹.. 2ⁿ⁻¹-1} ("2's complement")
 - char (8-bit), short (16-bit), int/long (32-bit), long long (64-bit)
 - Floats: IEEE representation,
 - **float** (32-bit: 1 sign, 8 exponent, 23 mantissa)
 - **double** (64-bit: 1 sign, 11 exponent, 52 mantissa)
 - Strings: char array, ASCII representation
- Memory layout
 - Stack for local, static for globals, heap for malloc'd stuff (must free!)

POINTERS, ARRAYS, AND MEMORY ~AGAIN~

The following slides re-state a lot of what we've covered but in a different way. We'll likely skip it for time, but you can use the slides as an additional reference.

```
public class Example {
  public static void swap (int x, int y) {
    int temp = x;
    x = y;
    y = temp;
  }
  public static void main (String[] args) {
    int a = 42;
    int b = 100;
    swap (a, b);
    System.out.println("a = " + a + " b = " + b);
What does this print? Why?
```

```
public class Example {
  public static void swap (int x, int y) {
    int temp = x;
    x = y;
    y = temp;
  public static void main (String[] args) {
    int a = 42;
    int b = 100;
 ⇒ swap (a, b);
    System.out.println("a = " + a + " b = " + b);
```

Stack

	main
a	42
b	100

What does this print? Why?

```
public class Example {
   public static void swap (int x, int y) {
   \Rightarrow int temp = x;
     x = y;
     y = temp;
   public static void main (String[] args) {
     int a = 42;
     int b = 100;
c0
    \Rightarrowswap (a, b);
     System.out.println("a = " + a + " b = " + b);
```

What does this print? Why?

Stack

	main
а	42
b	100

SWa	ap
Х	42
У	100
temp	333
RA	с0

```
public class Example {
   public static void swap (int x, int y) {
   \Rightarrow int temp = x;
     x = y;
     y = temp;
   public static void main (String[] args) {
     int a = 42;
     int b = 100;
c0
    \Rightarrowswap (a, b);
     System.out.println("a = " + a + " b = " + b);
```

What does this print? Why?

Stack

	main
а	42
b	100

swap						
42						
100						
42						
с0						

Let's do a little Java...

```
public class Example {
   public static void swap (int x, int y) {
     int temp = x;
   \Rightarrow x = y;
     y = temp;
   public static void main (String[] args) {
     int a = 42;
     int b = 100;
c0
    \Longrightarrowswap (a, b);
     System.out.println("a = " + a + " b = " + b);
```

What does this print? Why?

Stack

main		
a	42	
b	100	

swap		
100		
100		
42		
С0		

Let's do a little Java...

```
public class Example {
   public static void swap (int x, int y) {
     int temp = x;
     x = y;
   \Rightarrow y = temp;
   public static void main (String[] args) {
     int a = 42;
     int b = 100;
c0
    \Longrightarrowswap (a, b);
     System.out.println("a = " + a + " b = " + b);
```

What does this print? Why?

Stack

main		
a	42	
b	100	

swap		
X	100	
У	42	
temp	42	
RA	c0	
Y temp	42 42	

Let's do a little Java...

```
public class Example {
  public static void swap (int x, int y) {
    int temp = x;
    x = y;
    y = temp;
  public static void main (String[] args) {
    int a = 42;
    int b = 100;
    swap (a, b);
  \Rightarrow System.out.println("a =" + a + " b = " + b);
```

What does this print? Why?

Stack

	main
a	42
b	100

```
public class Ex2 {
  int data;
  public Ex2 (int d) { data = d; }
 public static void swap (Ex2 x, Ex2 y) {
    int temp = x.data;
    x.data = y.data;
    y.data = temp;
  public static void main (String[] args) {
   Example a = new Example (42);
    Example b = new Example (100);
    swap (a, b);
    System.out.println("a =" + a.data +
                       b = b + b.data;
```

Stack

main
a ??
b ??

```
public class Ex2 {
  int data;
  public Ex2 (int d) { data = d; }
 public static void swap (Ex2 x, Ex2 y) {
    int temp = x.data;
    x.data = y.data;
    y.data = temp;
  public static void main (String[] args) {
    Example a = new Example (42);
   Example b = new Example (100);
    swap (a, b);
    System.out.println("a =" + a.data +
                       b = b + b.data;
```

Stack

main

a
b ??

Lex2
data 42

```
Stack
                                                                  Heap
public class Ex2 {
  int data;
                                                 main
  public Ex2 (int d) { data = d; }
                                               а
                                                                  Ex2
  public static void swap (Ex2 x, Ex2 y) {
                                               b
                                                               data
                                                                      42
    int temp = x.data;
    x.data = y.data;
    y.data = temp;
  public static void main (String[] args) {
    Example a = new Example (42);
    Example b = new Example (100);
                                                                   Ex2
   swap (a, b);
                                                               data 100
    System.out.println("a =" + a.data +
                       b = b + b.data;
```

```
public class Ex2 {
                                                    Stack
                                                                    Heap
   int data;
                                                    main
   public Ex2 (int d) { data = d; }
                                                  а
                                                                     Ex2
   public static void swap (Ex2 x, Ex2 y) {
                                                  b
                                                                  data
   → int temp = x.data;
     x.data = y.data;
                                                    swap
     y.data = temp;
                                                  Х
                                                  У
                                                  temp
   public static void main (String[] args) {
                                                  RA
                                                        c0
     Example a = new Example (42);
     Example b = new Example (100);
                                                                     Ex2
c0
     >swap (a, b);
                                                                  data 100
     System.out.println("a =" + a.data +
                         b = b + b.data;
```

What does this print? Why?

42

```
public class Ex2 {
                                                    Stack
                                                                     Heap
   int data;
                                                    main
   public Ex2 (int d) { data = d; }
                                                  а
                                                                     Ex2
   public static void swap (Ex2 x, Ex2 y) {
                                                  b
                                                                  data
                                                                         42
   → int temp = x.data;
     x.data = y.data;
                                                    swap
     y.data = temp;
                                                  Х
                                                  У
                                                        42
                                                  temp
   public static void main (String[] args) {
                                                  RA
                                                        c0
     Example a = new Example (42);
     Example b = new Example (100);
                                                                     Ex2
c0
     >swap (a, b);
                                                                  data 100
     System.out.println("a =" + a.data +
                         b = b + b.data;
```

```
public class Ex2 {
                                                    Stack
                                                                    Heap
   int data;
                                                    main
   public Ex2 (int d) { data = d; }
                                                 а
                                                                     Ex2
   public static void swap (Ex2 x, Ex2 y) {
                                                 b
                                                                  data 100
     int temp = x.data;
    x.data = y.data;
                                                    swap
     y.data = temp;
                                                 Х
                                                 У
                                                 temp
   public static void main (String[] args) {
                                                 RΑ
                                                        c0
     Example a = new Example (42);
     Example b = new Example (100);
                                                                     Ex2
c0
     >swap (a, b);
                                                                  data 100
     System.out.println("a =" + a.data +
                         b = b + b.data;
```

```
public class Ex2 {
                                                    Stack
                                                                    Heap
   int data;
                                                    main
   public Ex2 (int d) { data = d; }
                                                  а
                                                                     Ex2
   public static void swap (Ex2 x, Ex2 y) {
                                                  b
                                                                  data 100
     int temp = x.data;
     x.data = y.data;
                                                    swap
     y.data = temp;
                                                  Х
                                                  У
                                                  temp
   public static void main (String[] args) {
                                                  RΑ
                                                        c0
     Example a = new Example (42);
     Example b = new Example (100);
                                                                     Ex2
c0
     >swap (a, b);
                                                                  data
                                                                         42
     System.out.println("a =" + a.data +
                         b = b + b.data;
```

```
Stack
                                                                  Heap
public class Ex2 {
  int data;
                                                  main
  public Ex2 (int d) { data = d; }
                                               а
                                                                   Ex2
  public static void swap (Ex2 x, Ex2 y) {
                                               b
                                                                data 100
    int temp = x.data;
    x.data = y.data;
    y.data = temp;
  public static void main (String[] args) {
    Example a = new Example (42);
    Example b = new Example (100);
                                                                   Ex2
    swap (a, b);
                                                                data
                                                                       42
    System.out.println("a =" + a.data +
                       b = b + b.data;
```

References and Pointers (review)

- Java has references:
 - Any variable of object type is a reference
 - Point at objects (which are all in the heap)
 - Under the hood: is the memory address of the object
 - Cannot explicitly manipulate them (e.g., add 4)
- Some languages (C,C++,assembly) have explicit pointers:
 - Hold the memory address of something
 - Can explicitly compute on them
 - Can de-reference the pointer (*ptr) to get thing-pointed-to
 - Can take the address-of (&x) to get something's address
 - Can do very unsafe things, shoot yourself in the foot

Pointers

- "address of" operator &
 - don't confuse with bitwise AND operator (&&)

<u>Given</u>

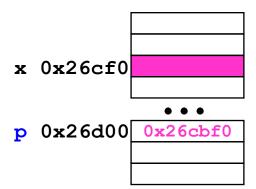
```
int x; int* p; // p points to an int
p = &x;

Then

*p = 2; and x = 2; produce the same result
Note: p is a pointer, *p is an int
```

• What happens for p = 2?;

On 32-bit machine, p is 32-bits



Back to Arrays

Java:
 int [] x = new int [nElems];
 C:
 int data[42]; //if size is known constant
 int* data = (int*)malloc (nElem * sizeof(int));
 malloc takes number of bytes
 sizeof tells how many bytes something takes

Arrays, Pointers, and Address Calculation

- x is a pointer, what is x+33?
- A pointer, but where?
 - what does calculation depend on?
- Result of adding an int to a pointer depends on size of object pointed to
 - One reason why we tell compiler what type of pointer we have, even though all pointers are really the same thing (and same size)

```
int* a=malloc(100*sizeof(int));
                  32
                     33
                            98
                               99
      a[33] is the same as *(a+33)
      if a is 0x00a0, then a+1 is
      0x00a4, a+2 is 0x00a8
       (decimal 160, 164, 168)
double* d=malloc(200*sizeof(double));
                       3
                                 199
      *(d+33) is the same as d[33]
      if d is 0x00b0, then d+1 is
      0x00b8, d+2 is 0x00c0
      (decimal 176, 184, 192)
```

More Pointer Arithmetic

- address one past the end of an array is ok for pointer comparison only
- what's at * (begin+44)?
- what does begin++ mean?
- how are pointers compared using < and using == ?
- what is value of end begin?

```
16
                     42
            15
                         43
char* a = new char[44];
char* begin = a;
char* end = a + 44;
while (begin < end)</pre>
   *begin = 'z';
   begin++;
```

More Pointers & Arrays

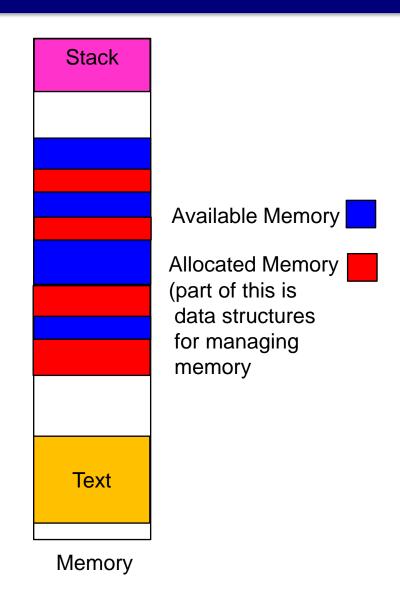
```
int* a = new int[100];
            /32 33
                     98 99
a is a poi/nter
*a is an/int
a[0] is/an int (same as *a)
a[1] i/s an int
a+1 ½s a pointer
a+32 is a pointer
*(a+1) is an int (same as a[1])
*(a+99) is an int
*(a+100) is trouble
```

Array Example

```
#include <stdio.h>
main()
{
  int* a = (int*)malloc (100 * sizeof(int));
  int* p = a;
  int k;
  for (k = 0; k < 100; k++)
     *p = k;
     p++;
  printf("entry 3 = %d\n'', a[3])
```

Memory Manager (Heap Manager)

- malloc() and free()
- Library routines that handle memory management for heap (allocation / deallocation)
- Java has garbage collection (reclaim memory of unreferenced objects)
- C must use free, else memory leak



Strings as Arrays (review)

```
s t r i g \( \lambda \) 0 1 15 16 42 43
```

- A string is an array of characters with '\0' at the end
- Each element is one byte, ASCII code
- '\0' is null (ASCII code 0)

strlen() again

- strlen() returns the number of characters in a string
 - same as number elements in char array?

```
int strlen(char * s)

// pre: '\0' terminated

// post: returns # chars
{
    int count=0;
    while (*s++)
        count++;
    return count;
}
```

Vector Class vs. Arrays

- Vector Class
 - insulates programmers
 - array bounds checking
 - automagically growing/shrinking when more items are added/deleted
- How are Vectors implemented?
 - Arrays, re-allocated as needed
- Arrays can be more efficient